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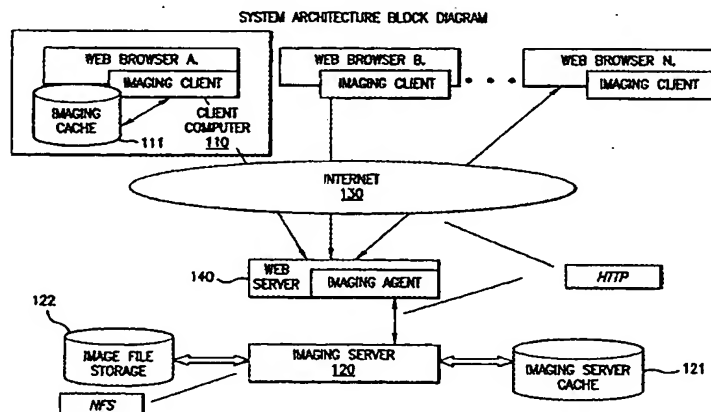
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(54) Title: SYSTEM AND METHOD FOR THE LOSSLESS PROGRESSIVE STREAMING OF IMAGES OVER A COMMUNICATION NETWORK



(57) Abstract: Disclosed is a lossless image streaming system for the transmission of images over a communication network. The system eliminates the necessity to store a compressed version of the original image, by losslessly streaming ROI data using the original stored image. The imaging system of the present invention also avoids the computationally intensive task of compression of the full image. When a user (110) wishes to interact with a remote image, the imaging server (120) performs a fast preprocessing step in near real time after which it can respond to any ROI requests also in near real time. When a ROI request arrives at the server, a sophisticated progressive image encoding algorithm is performed, but not for the full image. Instead, the encoding algorithm is performed only for the ROI. Since the size of the ROI is bounded by the size and resolution of the viewing device at the client and not by the size of the image, only a small portion of the full progressive coding computation is performed for a local area of the original image.

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For two-letter codes and other abbreviations, refer to the "Guidance Notes on Codes and Abbreviations" appearing at the beginning of each regular issue of the PCT Gazette.

5 **SYSTEM AND METHOD FOR THE LOSSLESS PROGRESSIVE STREAMING
OF IMAGES OVER A COMMUNICATION NETWORK**

 This application claims priority to U.S. Utility Patent Application No.
10 09/386,264 filed August 31, 1999, entitled "SYSTEM AND METHOD FOR
TRANSMITTING A DIGITAL IMAGE OVER A COMMUNICATION NETWORK",
and U.S. Provisional Patent Application No. 60/198,017, filed April 18, 2000, entitled
"LOSSLESS PROGRESSIVE STREAMING OF IMAGES OVER THE INTERNET",
the entirety of which are both incorporated herein by reference.

15

BACKGROUND OF THE INVENTION

20 **FIELD OF THE INVENTION**

 This invention relates to systems and methods for transmission of still images
over relatively low-speed communication channels. More specifically the invention
relates to progressive image streaming over low speed communication lines, and may
be applied to a variety of fields and disciplines, including commercial printing and
25 medical imaging, among others.

BRIEF DESCRIPTION OF THE PRIOR ART

30 In a narrow bandwidth environment, a simple transfer to the client computer of
any original image stored in the server's storage is obviously time consuming. In many
cases the user only wishes to view a low resolution of the image and perhaps a few
more high-resolution details, in these instances it would be inefficient to transfer the
full image. This problem can be overcome by storing images in some compressed
35 formats. Examples for such formats are standards such as Progressive JPEG (W.
Pennebaker and J. Mitchell, "JPEG, still image data compression standard", VNR,
1993) or the upcoming JPEG2000 (D. Taubman, "High performance scalable image
compression with EBCOT", preprint, 1999). These formats allow progressive
transmission of an image such that the quality of the image displayed at the client
40 computer improves during the transmission.

5 In some application such as medical imaging, it is also necessary that
 whenever the user at the client computer is viewing a portion of the highest resolution
 of the image, the progressive streaming will terminate at lossless quality. This means
 that at the end of progressive transmission the pixels rendered on the screen are exactly
 the pixels of the original image. The current known "state-of-the-art" wavelet
 10 algorithms for progressive lossless streaming all have a major drawback: their rate-
 distortion behavior is very inferior to the "lossy" algorithms. The implications are
 serious:

1. Whenever the user is viewing any low resolution of the image (at low
 15 resolutions the term "lossless" is not well defined) more data needs to be sent
 for the same visual quality.
2. During the progressive transmission of the highest resolution, before lossless
 quality is achieved, more data needs to be sent for the same visual quality.

20 Researchers working in this field are troubled by these phenomena. As F. Sheng, A.
 Bilgin, J. Sementilli and M. W. Marcellin say in [SBSM]: "...Improved lossy
 performance when using integer transforms is a pursuit of our on-going work." Here is
 an example:

25

Wavelet	Rate (bit per pixel)				
	0.1	0.2	0.5	0.7	1.0
Floating Point 7x9	24.18	26.65	31.64	34.17	36.90
Reversible (4,4)	23.89	26.41	31.14	33.35	35.65

30 **Table 1 – Comparison of the lossy compression performances
 (implemented by the (7,9) Wavelet) to a lossless compression
 (implemented by a reversible (4,4) Wavelet) of "Barabara" image
 (PSNR (dB)) ([SBSM]).**

5 As one can see from Table 1, state of the art progressive lossless coding is inferior to lossy coding by more than 1 dB at the high bit-rate.

 Indeed, intuitively, the requirement for lossless progressive image transmission should not effect the rendering of lower resolutions or the progressive "lossy" rendering of the highest resolution before lossless quality is obtained. The final lossless quality
10 should be a layer that in some sense is added to a lossy algorithm with minor (if any) effect on its performance.

 The main problem with known lossless wavelet algorithms, such as SPIHT [SP1] and CREW [ZASB], is that they use special "Integer To Integer" transforms (see "Wavelet transforms that map integers to integers", A. Calderbank, I. Daubechies, W.
15 Sweldens, B. L. Yeo, J. Fourier Anal. Appl., 1998). These transforms mimic "mathematically proven" transforms that work well in lossy compression using floating-point arithmetic implementations. But because they are constraint to be lossless, they do not approximate their floating-point ancestors sufficiently well. Although in all previous work there have been attempts to correct this approximation in
20 the progressive coding stage of the algorithm, the bad starting point, an inefficient transform, prevented previous authors to obtain decent rate-distortion behavior.

 Our algorithm solves the rate-distortion behavior problem. Using the fact that images are two-dimensional signals, we introduce new 2D lossless Wavelet transforms that approximate much better their lossy counterparts. As an immediate consequence
25 our lossless progressive coding algorithm has the same rate-distortion of a lossy algorithm during the lossy part of the progressive transmission.

SUMMARY OF THE INVENTION

 The imaging system that is described below is directed to a lossless image
30 streaming system that is different from traditional compression systems and overcomes the above problems. By utilizing a lossless means of progressive transmission means the pixels rendered on the screen at the end of transmission are exactly the pixels of the original image that was transmitted. The imaging system disclosed herein eliminates the necessity to store a compressed version of the original image, by streaming ROI
35 data using the original stored image. The imaging system of the present invention also avoids the computationally intensive task of compression of the full image. Instead,

5 once a user wishes to interact with a remote image, the imaging server performs a fast preprocessing step in near real time after which it can respond to any ROI requests also in near real time. When a ROI request arrives at the server, a sophisticated progressive image-encoding algorithm is performed, but not for the full image. Instead, the encoding algorithm is performed only for the ROI. Since the size of the ROI is bounded
10 by the size and resolution of the viewing device at the client and not by the size of the image, only a small portion of the full progressive coding computation is performed for a local area of the original image. This local property is also true for the client. The client computer performs decoding and rendering only for ROI and not the full image. This real time streaming or Pixels-On-Demand™ architecture requires different
15 approaches even to old ideas. For example, similarly to some prior art, the present imaging system is based on wavelets. But while in other systems wavelet bases are selected according to their coding abilities, the choice of wavelet bases in the present imaging system depends more on their ability to perform well in the real time framework. The system of the present invention supports several modes of progressive
20 transmission: by resolution, by accuracy and by spatial order.

BRIEF DESCRIPTION OF THE DRAWINGS

- Figure 1 is a system architecture block diagram.
- 25 Figure 2 is an imaging system workflow diagram.
- Figure 3 is a flow diagram representing a "lossless progressive by accuracy" request list for a ROI.
- Figure 4 is a diagram depicting the client "progressive by accuracy" workflow.
- Figure 5 is a diagram depicting the server workflow.
- 30 Figure 6 is a diagram describing the server-preprocessing step.
- Figure 7 is a diagram describing the low resolution encoding process.
- Figure 8 is a diagram describing the ROI high resolution processing.
- Figure 9 is a diagram depicting the local forward lossless wavelet transform.
- Figure 10 is a diagram depicting the local inverse lossless wavelet transform.
- 35 Figure 11 is a diagram depicting the progressive rendering steps.

5 Figure 12 is a diagram depicting a lossless subband tile wherein the spatial grouping of subband coefficients are at a given resolution and the halfbit matrix is associated with the hh_j subband.

 Figure 13 a diagram depicting the RGB \leftrightarrow YUV reversible conversion.

10 Figure 14 a diagram depicting a lossless last bit plane data block in which only hl and hh subband coefficients are scanned.

 Figure 15 is a sample pseudo-code of the encoding algorithm represented by: (a) Least significant bit plane scan pseudo-code (b) Half bit plane scan pseudo-code.

 Figure 16 is a sample pseudo-code of the decoding algorithm represented by: (a) Least significant bit plane scan pseudo-code (b) Half bit plane scan pseudo-code.

15 Figure 17 is a diagram depicting the curve defining the mapping from Original_Image_Depth-bit image to Screen_Depth-bit.

 Figure 18 is a diagram depicting the decomposition of one-dimensional signal x to the Low-subband s and the High-subband d and the separable decomposition of two-dimensional signal X into 4 matrices (subbands): LL, HL, LH and HH .

20 Figure 19 is a diagram depicting the first stage of the 2D separable transform step in the X-direction.

 Figure 20 is a diagram depicting the second stage of the 2D separable transform step in the Y-direction.

25 Figure 21 is a diagram depicting the application of the full 2D Wavelet transform.

 Figure 22 is a flow diagram representing the least significant bit plane scan of the encoding algorithm.

 Figure 23 is a flow diagram representing the least significant bit plane scan of the decoding algorithm.

30 Figure 24 is a flow diagram describing a bit plane significance scan of the server-encoding algorithm.

 Figure 25 is a flow diagram describing the subband tile extraction of the client progressive rendering process.

35 Figure 26 is a diagram depicting the preprocessing multi-resolution structure.

5

DETAILED DESCRIPTION OF THE INVENTION**1. NOTATION AND TERMINOLOGY**

The following notation is used throughout this document.

10

Term	Definition
4D	Four dimensional
FIR	Finite Impulse Response
FWT	Forward Wavelet Transform
GUI	Graphical User Interface
ID	Identification tag
IWT	Inverse Wavelet Transform
ROI	Region Of Interest
URL	Uniform Resource Locator
LSB	Least Significant Bit
RMS	Root Square Error
FP	Floating Point
PDF	Probability Distribution Function

The following terminology and definitions apply throughout this document.

Term	Definition
Rendering	Procedure to output/display a ROI of an image into a device such as a monitor, printer, etc.
Multiresolution	A pyramidal structure representing an image at dyadic resolutions, beginning with the original image as the highest resolution.
Subband Transform / subband coefficients	A method of decomposing an image (time domain) to frequency components (frequency domain). A representation of an image as a sum of differences between the dyadic resolutions of the image's multiresolution.
Wavelet Transform / Wavelet coefficients	A special case of Subband Transform.
Progressive Transmission	Transmitting a given image in successive steps, where each step adds more detail to the rendering of the image
Progressive Rendering	A sequence of rendering operations, each adding more detail.
Progressive by accuracy	Transmit/render strong features first (sharp edges), less significant features (texture) last
Progressive by resolution	Transmit/render low resolution first, high resolution last
Progressive by spatial order	Transmit/render top of image first, bottom of image last
Distributed database	A database architecture that can be used in a network environment

Subband/Wavelet tile	A group of subband/wavelet coefficients corresponding to a time-frequency localization at some given spatial location and resolution/frequency
Subband/Wavelet data block	An encoded portion of a subband/wavelet tile that corresponds to some accuracy layer

5

2. OVERVIEW OF THE INVENTION

Referring to Figure 1, a block diagram is provided depicting the various components of the imaging system in one embodiment. A client computer 110 is coupled to a server computer 120 through a communication network 130.

10 In one embodiment, the client computer 110 and server computer 120 may comprise a PC-type computer operating with a Pentium-class microprocessor, or equivalent. Each of the computers 110 and 120 may include a cache 111, 121 respectively as part of its memory. The server may include a suitable storage device 122, such as a high-capacity disk, CD-ROM, DVD, or the like.

15 The client computer 110 and server computer 120 may be connected to each other, and to other computers, through a communication network 130, which may be the Internet, an Intranet (e.g., a local area network), a wide-area network, or the like. Those having ordinary skill in the art will recognize that any of a variety of communication networks may be used to implement the present invention.

20 With reference to Figure 2, the system workflow is described. Using any browser type application, the user of the client computer 110 connects to the Web Server 140 or directly to the Imaging server 120 as described in Figure 1. He/she then selects, using common browser tools an image residing on the Image file storage 122. The corresponding URL request is received and processed by the Imaging Server 120.

25 In case results of previous computations previous computations on the image are not present in the Imaging Cache 121, the server performs a fast preprocessing algorithm (see §2.1) in a lossless mode. The result of this computation is inserted into the cache 121. Unlike other more "traditional" applications or methods which perform full progressive encoding of the image in an "offline" type method, the goal of the

30 preprocessing step is to allow the server, after a relatively fast computational step, to serve any ROI specified by the user of the client computer. For example, for a 15M grayscale medical image, using the described (software) server, installed on computer

5 with a Pentium processor, fast disk, running Windows NT, the preprocessing step 501 will typically take 3 seconds. This is by order of magnitude faster than a "full" compression algorithm such as [S], [SP1], [T]. Serving ROI is sometimes called "pixels-on-demand" which means a progressive transmission of any ROI of the image in "real-time", where the quality of the view improves with the transfer rate until
10 lossless view is received in the client side. Once the preprocessing stage is done, the server sends to the client a notification that the "image is ready to be served". The server also transmits the basic parameters associated with the image such as dimensions, color space, etc. Upon receiving this notification, the client can select any ROI of the image using standard GUI. The ROI is formulated in step 203 into a request
15 list that is sent to the server. Each such request corresponds to a data block (§4). The order of requests in the list corresponds to some progressive mode selected in the context of the application such as "progressive by accuracy" rendering of the ROI. Upon receiving the ROI request list, the server processes the requests according to their order. For each such request the server checks if the corresponding data block exists in
20 the Cache 121. If not, the server then computes the data block, stores it in the cache and immediately sends it to the client. Once a data block that was requested arrives at the client, it is inserted into the cache 111. At various points in time during the transfer process, a decision rule invokes a rendering of the ROI. Obviously, if some of the data blocks required for a high quality rendering of the ROI, were requested from the server,
25 but have not arrived yet, the rendering of the ROI will be of lower quality. But, due to the progressive request order, the rendering quality will improve with each received data block in an "optimal" way. In case the user changes the ROI, the rendering task at the client is canceled and a new request list corresponding to a new ROI, sent from the client to the server, will notify the server to terminate the previous computation and
30 transmission task and begin the new one.

3. NEW REVERSIBLE WAVELET TRANSFORM

35 We will now explain in detail why the rate-distortion behavior of our progressive lossless algorithm is better than other known algorithms. Lossless wavelet transform, must be integer-to-integer transform, such that round-off errors are avoided.

- 5 In order to demonstrate the difference between lossy and lossless transforms, let us look at the simplest wavelet, the Haar wavelet. Let $x(k)$ be the k -th component of the one-dimensional discrete signal x . The first forward Haar transform step, in its accurate “mathematical” form, is defined by:

$$10 \quad \begin{cases} s(n) = \frac{1}{\sqrt{2}}(x(2n+1) + x(2n)), \\ d(n) = \frac{1}{\sqrt{2}}(x(2n+1) - x(2n)), \end{cases} \quad (3.1)$$

where s is a low-resolution version of x , and d is the “difference” between s and x . In the case of lossless transform, applying the above transform results in round-off error. One possibility is to apply the transform step suggested by [CDSI]:

$$15 \quad \begin{cases} s(n) = \left\lfloor \frac{x(2n+1) + x(2n)}{2} \right\rfloor, \\ d(n) = x(2n+1) - x(2n). \end{cases} \quad (3.2)$$

The symbol $\lfloor \circ \rfloor$ is the floor function meaning “greatest integer less than or equal to \circ ”,
 20 e.g.
 $\lfloor 0.5 \rfloor = 0$, $\lfloor -1.5 \rfloor = -1$, $\lfloor 2 \rfloor = 2$, $\lfloor -1 \rfloor = -1$.

The one-dimensional transform step is generalized to 2D separable transform step, by applying the 1D transform step twice, first in the X-direction and then (on the
 25 first stage output) in the Y-direction as described in Figure 18, 19 and 20 (see also [M] 7.7). The full 2D Wavelet transform is applied by using the 2D Wavelet transform step iteratively in the classic Mallat decomposition of the image (Figure 21) ([M] 7.7).

In (3.2) two properties are kept:

- 30 1. **Reversibility**, i.e., one can restore $x(2n)$ and $x(2n+1)$, by knowing $s(n)$ and $d(n)$, as follows:

$$\begin{cases} x(2n) = s(n) - \left\lfloor \frac{d(n)}{2} \right\rfloor, \\ x(2n+1) = d(n) + x(2n). \end{cases} \quad (3.3)$$

2. **De-correlation**, i.e., $s(n)$ and $d(n)$ contains the minimal number of bits required in order to follow property 1. For example, if the transform would have been defined by:

$$\begin{cases} s(n) = x(2n+1) + x(2n), \\ d(n) = x(2n+1) - x(2n), \end{cases} \quad (3.4)$$

then the least significant bit of $s(n)$ and $d(n)$ would have been the same and saved twice. In other words, there is a correlation between $s(n)$ and $d(n)$ in (3.4). From the view point of coding this should be avoided since there is a redundancy of transmitting this bit.

On the other hand, the **scaling** property, that is a very important one, is not kept in (3.2). Observe that the value of $s(n)$ computed by (3.2), is smaller than its "real mathematical value" as computed in (3.1), by factor of $\sqrt{2}$. Since $s(n)$ should be rounded to an integer number, the fact that $s(n)$ is smaller than what it should be, increases the round-off error. In low resolutions, the error is accumulated through the wavelet steps.

If we take the error as a model of "white noise" added to the i -th resolution in a multi-resolution representation of the image, i.e. X_i in Figure 21, it can be proved that the variance of this noise exponentially increases as a function of i . This "contamination" to the multi-resolution image damages the coding efficiency at low bit-rates. Let us describe this in detail for the case of the Haar wavelet. We have two assumptions in our analysis:

1. The parity (least significant bit) of an arbitrary coefficient c , in any of the wavelet steps is a uniformly distributed random variable, i.e.

$$\Pr(c \equiv 0 \pmod{2}) = \Pr(c \equiv 1 \pmod{2}) = \frac{1}{2}.$$

- 5 2. This parity is independent of other coefficient's parity (Identically independent distributed).

Our referenced computation, i.e. the accurate computation, is the Haar transform step defined in (3.1). We concentrate on the LL-subband coefficients, because the low-
 10 resolution subbands are computed from them. LL-subband coefficients are the result of a 2D-transform step (Figure 18)

$$ll^{(\text{accurate})}(m,n) = \frac{x(2m+1,2n+1) + x(2m,2n+1) + x(2m+1,2n) + x(2m,2n)}{2},$$

where m and n are the indices of the row and column of the coefficient respectively.

- 15 As described in Figure 18, 19 and 20, according to the step defined in (3.2), we first apply the X-direction step

$$s(k,n) = \left\lfloor \frac{x(k,2n+1) + x(k,2n)}{2} \right\rfloor,$$

for each input row $x(k,\cdot)$.

20

Under assumption 1 mentioned above, we can write $s(k,n)$ as

$$\dot{s}(k,n) = \frac{x(k,2n+1) + x(k,2n)}{2} + e, \quad (3.5)$$

- 25 where e is a random variable with a probability distribution function (P.D.F.) $p(\cdot)$ defined by

$$\begin{cases} p(-0.5) = \Pr(e = -0.5) = \frac{1}{2}, \\ p(0) = \Pr(e = 0) = \frac{1}{2}. \end{cases} \quad (3.6)$$

Therefore,

$$30 \quad \quad \quad E(e) = -\frac{1}{4}, \text{Var}(e) = \frac{1}{16}. \quad (3.7)$$

5 We then apply the Y-direction transform by

$$10 \quad H^{(\text{CDSI})}(m, n) = \left\lfloor \frac{s(2m+1, n) + s(2m, n)}{2} \right\rfloor = \frac{s(2m+1, n) + s(2m, n)}{2} + e'. \quad (3.8)$$

As in (3.5) we can represent $s(2m+1, n)$ and $s(2m, n)$ by:

$$s(2m+1, n) = \frac{x(2m+1, 2n+1) + x(2m+1, 2n)}{2} + e_1, \quad (3.9)$$

$$s(2m, n) = \frac{x(2m, 2n+1) + x(2m, 2n)}{2} + e_2. \quad (3.10)$$

Now we can write:

$$\begin{aligned} 15 \quad H^{(\text{CDSI})}(m, n) &= \frac{\frac{x(2m+1, 2n+1) + x(2m+1, 2n)}{2} + e_1 + \frac{x(2m, 2n+1) + x(2m, 2n)}{2} + e_2}{2} + e' \\ &= \frac{x(2m+1, 2n+1) + x(2m+1, 2n) + x(2m, 2n+1) + x(2m, 2n)}{4} + \frac{e_1}{2} + \frac{e_2}{2} + e' \\ &= \frac{x(2m+1, 2n+1) + x(2m+1, 2n) + x(2m, 2n+1) + x(2m, 2n)}{4} + e \end{aligned} \quad (3.11)$$

where e_1, e_2, e' are independent (assumption 2 above) random variables with

20 expectation $\frac{1}{4}$, Variance $\frac{1}{16}$, and $e = \frac{e_1}{2} + \frac{e_2}{2} + e'$.

Therefore,

$$E(e) = \frac{1}{2}E(e_1) + \frac{1}{2}E(e_2) + E(e') = -\frac{1}{2},$$

$$\begin{aligned} \text{Var}(e) &= \text{Var}\left(\frac{e_1}{2} + \frac{e_2}{2} + e'\right) = \frac{1}{4}\text{Var}(e_1) + \frac{1}{4}\text{Var}(e_2) + \text{Var}(e') = \\ &= \frac{1}{4} \cdot \frac{1}{16} + \frac{1}{4} \cdot \frac{1}{16} + \frac{1}{16} = \frac{3}{32}. \end{aligned} \quad (3.12)$$

Thus,

$$l^{(\text{CDSI})}(m, n) = \frac{l^{(\text{accurate})}(m, n)}{2} + e. \quad (3.13)$$

e represents the approximation error of the LL-subband coefficients, results from one 2D transform step. The error relates to the accurate floating-point computation.

This was a description of a single 2D-transform step assuming that the input coefficients are without any error. Now we wish to evaluate the error accumulated after several steps.

At an arbitrary step $i \geq 0$, we can assume that an input coefficient can be written as:

$$x_i(k, l) = x_i^{(\text{accurate})}(k, l) + e_i,$$

where $x_i^{(\text{accurate})}(k, l)$ is the accurate value achieved by floating-point computation for all the previous steps, i.e., a step defined by

$$\begin{cases} s(n) = \frac{x(2n+1) + x(2n)}{2}, \\ d(n) = x(2n+1) - x(2n), \end{cases} \quad (3.14)$$

instead of the integer-to-integer computation in (3.2). Observe that if $x_i^{(\text{accurate})}(k, l)$ is the i -th resolution image coefficient, using (3.14) as the 1D Wavelet step, then

$$x_i^{(\text{accurate})}(k, l) = \frac{l_{i-1}^{(\text{accurate})}(k, l)}{2^i}, \quad i \geq 1, \quad (3.15)$$

where $l_{i-1}^{(\text{accurate})}(k, l)$ is the normalized $(L_2 - \text{norm})$ LL-subband coefficient resulting from the i -th 2D transform step using (3.1) as the 1D Wavelet step (see Figure). e_i is

- 5 the difference between $x_i(k, l)$ and $x_i^{(\text{accurate})}(k, l)$ (I.e., the approximation error of the integer computation made until now). E.g. $e_0 = 0$ ($x_0(k, l)$ is an original image pixel), while e_i is a random number with expectation $-\frac{1}{2}$ and variance $\frac{3}{32}$ (see (3.12)).
- 0.

10

Using (3.11), we get:

$$\begin{aligned}
 & H_i^{(\text{CDSI})}(m, n) \\
 &= \frac{x_i^{(\text{acc})}(2m+1, 2n+1) + e_i^1 + x_i^{(\text{acc})}(2m+1, 2n) + e_i^2 + x_i^{(\text{acc})}(2m, 2n+1) + e_i^3 + x_i^{(\text{acc})}(2m, 2n) + e_i^4}{4} + e \\
 &= \frac{x_i^{(\text{acc})}(2m+1, 2n+1) + x_i^{(\text{acc})}(2m+1, 2n) + x_i^{(\text{acc})}(2m, 2n+1) + x_i^{(\text{acc})}(2m, 2n)}{4} + \frac{e_i^1 + e_i^2 + e_i^3 + e_i^4}{4} + e \\
 &= \frac{x_i^{(\text{acc})}(2m+1, 2n+1) + x_i^{(\text{acc})}(2m+1, 2n) + x_i^{(\text{acc})}(2m, 2n+1) + x_i^{(\text{acc})}(2m, 2n)}{4} + e_{i+1} \\
 &= x_{i+1}^{(\text{accurate})} + e_{i+1},
 \end{aligned}$$

where e_{i+1} is defined by

15

$$e_{i+1} = \frac{e_i^1 + e_i^2 + e_i^3 + e_i^4}{4} + e,$$

and corresponds to LL_i subband.

Consequently

$$\begin{aligned}
 E(e_{i+1}) &= E(e_i) + E(e), \\
 \text{Var}(e_{i+1}) &= \frac{\text{Var}(e_i)}{4} + \text{Var}(e).
 \end{aligned}$$

Observe that

20

$$E(e) = -\frac{1}{2}, \text{Var}(e) = \frac{3}{32}.$$

As a result, we can write recursive formulas for the error expectation and variance after i steps.

$$\begin{cases} E(e_0) = 0, \\ E(e_{i+1}) = E(e_i) - \frac{1}{2}, \\ \text{Var}(e_0) = 0, \\ \text{Var}(e_{i+1}) = \frac{\text{Var}(e_i)}{4} + \frac{3}{32}, \end{cases} \quad (3.16)$$

The explicit solutions to these formulas are

$$E(e_i) = -\frac{i}{2}, \text{Var}(e_i) = \frac{1}{8} - \frac{1}{2 \cdot 4^{i+1}}. \quad (3.17)$$

By replacing $x_i^{(\text{accurate})}(m, n)$ with $\frac{l_i^{(\text{accurate})}(m, n)}{2^i}$ we get

$$l_i^{(\text{CDSI})}(m, n) = \frac{l_i^{(\text{accurate})}(m, n)}{2^{i+1}} + e_{i+1}. \quad (3.18)$$

Thus, the approximation to $l_i^{(\text{accurate})}(m, n)$ is

$$2^{i+1} l_i^{(\text{CDSI})}(m, n) = l_i^{(\text{accurate})}(m, n) + 2^{i+1} e_{i+1}.$$

The approximation error expectation is

$$E(2^i e_i) = 2^i E(e_i) = 2^i \left(-\frac{i}{2} \right) = -i 2^{i-1}.$$

The approximation error variance and standard deviation are

$$\text{Var}(2^i e_i) = 4^i \text{Var}(e_i) = 4^i \left(\frac{1}{8} - \frac{1}{2 \cdot 4^{i+1}} \right) = \frac{4^i - 1}{8} \approx \frac{4^i}{8} = 2^{2i-3}.$$

Hence

$$\text{Std}(2^i e_i) = \sqrt{\text{Var}(2^i e_i)} \approx \frac{2^{i-1}}{\sqrt{2}}.$$

5

Let us now evaluate the approximation error of the 3 other subbands:

$$lh_i^{(\text{CDSI})}(m, n) = \left[\frac{lh_{i-1}^{(\text{CDSI})}(2m+1, 2n+1) + lh_{i-1}^{(\text{CDSI})}(2m+1, 2n)}{2} \right] - \left[\frac{lh_{i-1}^{(\text{CDSI})}(2m, 2n+1) + lh_{i-1}^{(\text{CDSI})}(2m, 2n)}{2} \right]$$

$$= \frac{lh_i^{(\text{accurate})}(m, n)}{2^i} + \frac{e_i^1 + e_i^2}{2} + e' - \left(\frac{e_i^3 + e_i^4}{2} + e'' \right) = \frac{lh_i^{(\text{accurate})}(m, n)}{2^i} + e_i^{LH}$$

where

10

- e_i^k $1 \leq k \leq 4$ are identical to the random variable whose expectation and variance are given in (3.17).
- $e_i^{LH} = \frac{e_i^1 + e_i^2}{2} + e' - \left(\frac{e_i^3 + e_i^4}{2} + e'' \right)$
- e' and e'' are identical to the random variable whose expectation and variance are given in (3.7).

15 Thus,

$$E(e_i^{LH}) = 0,$$

$$\begin{aligned} \text{Var}(e_i^{LH}) &\approx \frac{1}{4} \left(\frac{1}{8} - \frac{1}{2 \cdot 4^{i+1}} + \frac{1}{8} - \frac{1}{2 \cdot 4^{i+1}} \right) + \frac{1}{16} \\ &+ \frac{1}{4} \left(\frac{1}{8} - \frac{1}{2 \cdot 4^{i+1}} + \frac{1}{8} - \frac{1}{2 \cdot 4^{i+1}} \right) + \frac{1}{16} \\ &= \frac{1}{4} - \frac{1}{2 \cdot 4^{i+1}}. \end{aligned} \quad (3.19)$$

The approximation to $lh_i^{(\text{accurate})}(m, n)$ is

20

$$2^i lh_i^{(\text{CDSI})}(m, n) = lh_i^{(\text{accurate})}(m, n) + 2^i e_i^{LH}.$$

The approximation error variance and standard deviation are:

$$\text{Var}(2^i e_i^{LH}) = 4^i \text{Var}(e_i^{LH}) = 4^i \cdot \left(\frac{1}{4} - \frac{1}{2 \cdot 4^{i+1}} \right) = 4^{i-1} - \frac{1}{8} \approx 4^{i-1}.$$

Therefore

$$5 \quad \text{Std}(2^i e_i^{LH}) = \sqrt{\text{Var}(2^i e_i^{LH})} \approx \sqrt{4^{i-1}} = 2^{i-1}.$$

A similar approximation error estimation, it can be done with the HL-subband and the HH-subband.

10 The approximation error evaluation results are summarized in the following table where the error is the difference between the normalized (in L_2 -norm) coefficients according to [CDSI] reversible transform and the "mathematical" transform (defined in (3.1)).

	Expectation	Variance	Std
LL_i - error	$-(i+1)2^i$	$\frac{4^{i+1}-1}{8} \approx 2^{2i-1}$	$0.707 \cdot 2^i$
LH_i - error	0	$\frac{2 \cdot 4^i - 1}{8} \approx 4^{i-1}$	$0.5 \cdot 2^i$
HL_i - error	$-\frac{1}{4} \cdot 2^i$	$\frac{3 \cdot 4^i - 2}{16} \approx 3 \cdot 4^{i-2}$	$0.433 \cdot 2^i$
HH_i - error	0	$\frac{4^i - 1}{8} \approx 2^{2i-3}$	$0.354 \cdot 2^i$

15 **Table 2 - Normalized (in L_2 -norm) approximation errors of the Wavelet coefficients at resolution $i \geq 0$ ($i=0$ is the highest resolution) using the (CDSI) reversible Haar transform.**

20 Assuming a low-bit rate transmission where only the coefficients whose absolute value belongs to the range $[2^b, 2^{b+1})$ are encoded, for every resolution i , where i is greater than b (less or more). It must be noted that the large error implies a significant loss of coding efficiency.

Instead, we propose a new family of reversible transforms. The proposed family of integer wavelet transforms has all three properties:

25 **1. Reversibility**

5 2. De-correlation

3. Scaling – i.e. improved approximation of the “mathematical” transform.

Our 2D transform step is separable also, but the one-dimensional transform step, which the 2D transform is based on, is different for the X-direction (step 1901), the Y-direction step applied on the low output of the X-direction step (step 2001) and
 10 the Y-direction step applied on the high output of the X-direction step (step 2002) as described in Figure 18, 19 and 20.

The full 2D Wavelet transform is applied by using the 2D Wavelet transform step iteratively in the classic Mallat decomposition of the image (Figure 21) ([M] 7.7). As mentioned before, the Wavelet coefficients in our proposed transform are all scaled,
 15 i.e. normalized in L_2 – norm as the Wavelet coefficients computed in the accurate “mathematical” transform.

In order to achieve the third property (improved approximation of the “mathematical” transform), we define an extra matrix we call the “Half bit-matrix” which enables the reversibility of the High Y-transform step (step 2002). The elements
 20 that belong to this matrix are bits, such that each bit corresponds to an HH-subband coefficient in the following interpretation. Let us describe this by the following example.

Supposing

$$s(n) = 7, d^{(1)}(n) = 9$$

25 are a coefficient pair results from a reversible de-correlated 1D-wavelet step

$$\begin{cases} d^{(1)}(n) = x(2n+1) - x(2n), \\ s(n) = \left\lfloor \frac{x(2n) + x(2n+1)}{2} \right\rfloor. \end{cases}$$

Now, $d^{(1)}(n)$ has to be multiplied by $\frac{1}{2}$, in order to be scaled.

The binary form of $d^{(1)}(n) = 9$ is

$$d^{(1)}(n) = 1001_2.$$

30 If we now divide $d^{(1)}(n)$ by 2 in a floating-point computation we get

$$d^{FP}(n) = \frac{1}{2} d^{(1)}(n) = 100.1_2.$$

5

Let us call the bit, which located on the write-side of the floating point the "Half Bit". Observe that the Half Bit of $d^{FP}(n)$ is the LSB of $d^{(l)}(n)$. Therefore, an equivalent way to do this in an integer computation without losing the Half-Bit is to calculate first the LSB of $d^{(l)}(n)$ by

10

$$HalfBit(n) = d^{(l)}(n) \bmod 2 = 9 \bmod 2 = 1,$$

then to shift-write $d^{(l)}(n)$ by

$$d(n) = d^{(l)}(n) \gg 1 = 1001 \gg 1 = 100.$$

By saving $d(n)$ and $HalfBit(n)$ we can restore back $d^{(l)}(n)$.

15

In the proposed transform, this Half-bit is needed in the HH-subband coefficient computation. Therefore in our wavelet decomposition for every HH-subband coefficient (in all scales) there is a corresponding bit, which is the coefficient's Half-bit.

20

The Half bit matrix is hidden in the HH-subband in the description of Figure 18, 19 and 20. It is described explicitly in the specification of the transform as much in the coding algorithm.

We now present our integer-to-integer versions of the Haar transform and the CDF (1,3) transform for the 2-dimensional case.

3.1 Reversible Haar and (CDF) (1,3) Transforms

25

3.1.1 Haar Transform

With respect to Figure 19:

3.1.1.1 Step 1901: X-direction

30

Forward Step

$$\begin{cases} s(n) = \left\lfloor \frac{x(2n) + x(2n+1)}{2} \right\rfloor, \\ d(n) = x(2n+1) - x(2n). \end{cases} \quad (3.20)$$

5

Inverse Step

$$\begin{cases} x(2n) = s(n) - \left\lfloor \frac{d(n)}{2} \right\rfloor, \\ x(2n+1) = d(n) + x(2n). \end{cases} \quad (3.21)$$

With respect to Figure 20:

3.1.1.2 Step 2001: Y-direction – Low Forward Step

10

$$\begin{cases} s(n) = x(2n) + x(2n+1), \\ d^{(1)}(n) = \left\lfloor \frac{x(2n+1) - x(2n)}{2} \right\rfloor, \\ d(n) = 2d^{(1)}(n). \end{cases} \quad (3.22)$$

Remarks:

1. $s(n)$ is a scaled LL-subband coefficient.
2. $s(n)$ and $d^{(1)}(n)$ are de-correlated and a reversible couple (can be transformed back to $x(2n)$ and $x(2n+1)$), but $d^{(1)}(n)$ is not scaled (it is half its “real value”). Thus, $d^{(1)}(n)$ is multiplied by 2. Nevertheless, the LSB of the LH-subband coefficient $d(n)$ is known to be 0 and not encoded.

15

Inverse Step

$$\begin{cases} x(2n+1) = \frac{1}{2}(s(n) + d(n) + (s(n) \bmod 2)), \\ x(2n) = s(n) - x(2n+1). \end{cases} \quad (3.23)$$

20

With respect to Figure 20:

25

5 3.1.1.3 Step 2002: Y-direction – High Forward Step

$$\begin{cases} d^{(1)}(n) = x(2n+1) - x(2n), \\ \text{HalfBit}(n) = (d^{(1)}(n)) \bmod 2, \\ d(n) = \left\lfloor \frac{d^{(1)}(n)}{2} \right\rfloor, \\ s(n) = x(2n) + d(n). \end{cases} \quad (3.24)$$

Remark: $d^{(1)}(n)$ and $s(n)$ are de-correlated and reversible couples, but $d^{(1)}(n)$ is not scaled (It is twice its “real value”). Therefore, $d^{(1)}(n)$ is divided by 2. By doing that, we lose its least significant bit, which cannot be restored. To solve this problem, as explained before, we save this bit as the “Half-Bit”. Giving this name to that coefficient means that its weight is $\frac{1}{2}$ in the “real mathematical scale”, and it is the least significant (from the approximation point of view).

Inverse Step

$$\begin{cases} x(2n) = s(n) - d(n), \\ d^{(1)}(n) = 2d(n) + \text{HalfBit}(n), \\ x(2n+1) = d^{(1)}(n) + x(2n). \end{cases} \quad (3.25)$$

15

20

25

5 3.1.2 CDF (1,3) Transform

3.1.2.1 Step 1901: X-direction

With respect to Figure 19:

Forward Step

$$\begin{cases} s(n) = \left\lfloor \frac{x(2n) + x(2n+1)}{2} \right\rfloor, \\ d^{(1)}(n) = x(2n+1) - x(2n), \\ d(n) = d^{(1)}(n) + \left\lfloor \frac{s(n-1) - s(n+1)}{4} \right\rfloor. \end{cases} \quad (3.26)$$

Inverse Step

$$\begin{cases} d^{(1)}(n) = d(n) - \left\lfloor \frac{s(n-1) - s(n+1)}{4} \right\rfloor, \\ x(2n) = s(n) - \left\lfloor \frac{d^{(1)}(n)}{2} \right\rfloor, \\ x(2n+1) = x(2n) + d^{(1)}(n). \end{cases} \quad (3.27)$$

With respect to Figure 20:

3.1.2.2 Step 2001: Y-direction – Low Forward Step

$$\begin{cases} s(n) = x(2n) + x(2n+1), \\ d^{(1)}(n) = \left\lfloor \frac{x(2n+1) - x(2n) + \left\lfloor \frac{s(n-1) - s(n+1)}{8} \right\rfloor}{2} \right\rfloor, \\ d(n) = 2d^{(1)}(n). \end{cases} \quad (3.28)$$

Remark: See remarks for (3.22).

5

Inverse Step

$$\begin{cases} s^{(1)}(n) = s(n) - \left\lfloor \frac{s(n-1) - s(n+1)}{8} \right\rfloor, \\ x(2n+1) = \frac{1}{2} \left(s^{(1)}(n) + d(n) + (s^{(1)}(n) \bmod 2) \right), \\ x(2n) = s(n) - x(2n+1). \end{cases} \quad (3.29)$$

With respect to Figure 20:

10 **3.1.2.3 Step 2002: Y-direction – High Forward Step**

$$\begin{cases} s(n) = \left\lfloor \frac{x(2n) + x(2n+1)}{2} \right\rfloor, \\ d^{(1)}(n) = x(2n+1) - x(2n), \\ d^{(2)}(n) = d^{(1)}(n) + \left\lfloor \frac{s(n-1) - s(n+1)}{4} \right\rfloor, \\ d(n) = \left\lfloor \frac{d^{(2)}(n)}{2} \right\rfloor, \\ HalfBit(n) = d^{(2)}(n) \bmod 2. \end{cases} \quad (3.30)$$

Inverse Step

$$\begin{cases} d^{(1)}(n) = 2d(n) + HalfBit(n) - \left\lfloor \frac{s(n-1) - s(n+1)}{4} \right\rfloor, \\ x(2n) = s(n) - \left\lfloor \frac{d^{(1)}(n)}{2} \right\rfloor, \\ x(2n+1) = d^{(1)}(n) + x(2n). \end{cases} \quad (3.31)$$

15

We now compute the approximation error probabilities of our method, and show that it is significantly smaller. We start with the LL-subband error. Assuming e_i

- 5 is the approximation error of the LL-subband in the i -th resolution (Figure 21), the LL-subband coefficient in the i -th resolution can be written as:

$$\begin{aligned}
 l_i^{(new)}(m, n) &= \left\lfloor \frac{x_i^{(new)}(2m+1, 2n+1) + x_i^{(new)}(2m, 2n+1)}{2} \right\rfloor \\
 &+ \left\lfloor \frac{x_i^{(new)}(2m+1, 2n) + x_i^{(new)}(2m, 2n)}{2} \right\rfloor \\
 &= \frac{x_i^{(acc)}(2m+1, 2n+1) + e_{i-1}^1 + x_i^{(acc)}(2m, 2n+1) + e_{i-1}^2}{2} + e' \\
 &+ \frac{x_i^{(acc)}(2m+1, 2n) + e_{i-1}^3 + x_i^{(acc)}(2m, 2n) + e_{i-1}^4}{2} + e'' \\
 &= \frac{x_i^{(acc)}(2m+1, 2n+1) + x_i^{(acc)}(2m, 2n+1) + x_i^{(acc)}(2m+1, 2n) + x_i^{(acc)}(2m, 2n)}{2} \\
 &+ \frac{e_{i-1}^1 + e_{i-1}^2 + e_{i-1}^3 + e_{i-1}^4}{2} + e' + e'' = \\
 &= l_i^{(acc)}(m, n) + e_i,
 \end{aligned} \tag{3.32}$$

where

- 10 • $l_i^{(new)}(m, n)$ is the new transform LL-subband coefficient (i -th resolution).
- e_{i-1}^k for $1 \leq k \leq 4$, are identical random variable representing the error from the previous level.
- e' and e'' are random variables with P.D.F. defined in (3.6).
- $x_i^{(acc)}(m, n)$ is the i -th resolution image coefficient using (3.1) as the 1D
- 15 Wavelet step.
- $l_i^{(acc)}(m, n)$ is the normalized (L_2 -norm) LL-subband coefficient resulting from the i -th 2D transform step using (3.1) as the 1D Wavelet step (see Figure 21).
- $e_i = \frac{e_{i-1}^1 + e_{i-1}^2 + e_{i-1}^3 + e_{i-1}^4}{2} + e' + e''$.
- 20

Consequently

$$E(e_i) = \frac{4E(e_{i-1})}{2} + \left(-\frac{1}{4}\right) + \left(-\frac{1}{4}\right) = 2E(e_{i-1}) - \frac{1}{2}, \tag{3.33}$$

$$\text{Var}(e_i) = \frac{4\text{Var}(e_{i-1})}{4} + \frac{1}{16} + \frac{1}{16} = \text{Var}(e_{i-1}) + \frac{1}{8}. \tag{3.34}$$

5

By knowing that $e_{-1} = 0$ we get

$$\begin{cases} E(e_i) = \frac{1}{2} - 2^i, \\ \text{Var}(e_i) = \frac{i+1}{8}. \end{cases} \quad (3.35)$$

Now we can easily evaluate the approximation error of the 3 other subbands:

$$\begin{aligned} & lh_i^{(new)}(m, n) \\ &= 2 \left[\frac{x_i^{(new)}(2m+1, 2n+1) + x_i^{(new)}(2m, 2n+1)}{2} - \frac{x_i^{(new)}(2m+1, 2n) + x_i^{(new)}(2m, 2n)}{2} \right] \end{aligned} \quad (3.36)$$

10

$$\begin{aligned} &= \frac{(x_i^{(acc)}(2m+1, 2n+1) + x_i^{(acc)}(2m, 2n+1)) - (x_i^{(acc)}(2m+1, 2n) + x_i^{(acc)}(2m, 2n))}{2} \\ &+ \frac{e_{i-1}^1 + e_{i-1}^2 - e_{i-1}^3 - e_{i-1}^4}{2} + e' - e'' + 2e''' \\ &= lh_i^{(acc)}(m, n) + e_i^{LH}, \end{aligned}$$

where

- 15 • $lh_i^{(new)}(m, n)$ is the new transform LH-subband coefficient (i -th resolution).
- $lh_i^{(accurate)}(m, n)$ is the normalized (L_2 -norm) LH-subband coefficient resulting from the i -th 2D transform step using (3.1) as the 1D Wavelet step (see Figure 21).
- e''' is a random variable with P.D.F. defined in (3.6).
- 20 • $e_i^{LH} = \frac{e_{i-1}^1 + e_{i-1}^2 - e_{i-1}^3 - e_{i-1}^4}{2} + e' - e'' + 2e'''$
- all other symbols are defined like in (3.32).

5 Hence

$$E(e_i^{LH}) = \frac{2E(e_{i-1}) - 2E(e_{i-1})}{2} + \left(-\frac{1}{4}\right) - \left(-\frac{1}{4}\right) + 2 \cdot \left(-\frac{1}{4}\right) = -\frac{1}{2}, \quad (3.37)$$

$$\text{Var}(e_i^{LH}) = \frac{4\text{Var}(e_{i-1})}{4} + \frac{1}{16} + \frac{1}{16} + 4 \cdot \frac{1}{16} = \frac{i+3}{8}. \quad (3.38)$$

Similar estimation can be done for the HL and the HH subbands.

10 The error estimation (for all subbands) are summarized in the following table where the error is the difference between the normalized (in L_2 -norm) coefficients according to our new reversible transform and the "mathematical" transform (defined in (3.1)).

	Expectation	Variance	Std
LL_i - error	$\frac{1}{2} - 2^i$	$\frac{i+1}{8}$	$\sqrt{\frac{i+1}{8}}$
LH_i - error	$-\frac{1}{2}$	$\frac{i+3}{8}$	$\sqrt{\frac{i+3}{8}}$
HL_i - error	$-\frac{1}{4}$	$\frac{i}{8} + \frac{1}{16}$	$\sqrt{\frac{i}{8} + \frac{1}{16}}$
HH_i - error	$-\frac{1}{4}$	$\frac{i}{8} + \frac{1}{16}$	$\sqrt{\frac{i}{8} + \frac{1}{16}}$

15

Table 3 - Normalized (in L_2 -norm) approximation errors of the Wavelet coefficients at resolution $i \geq 0$ ($i=0$ is the highest resolution) using the proposed reversible Haar transform. The result for the LL-subband is valid for the proposed reversible (1,3) transform also.

20

The meaning of this result is that in a low bit-rate, where only large coefficients are encoded, this error is negligible.

25

5 4. IMAGING PROTOCOL AND DISTRIBUTED DATABASE

Dividing the data into tiles and bit-planes

For the purpose of efficient rendering the coefficients may be sub-divided into tiles. The tiles of this invention differ from previous art as shown in Figure 12. As in
 10 the lossy algorithm, here also the subband tiles are further decomposed to subband data blocks. Each data block of lossless subband tile (Figure 12) will have a 4D coordinate

$$(t_x, t_y, t_resolution, t_bitPlane)$$

where $0 \leq t_bitPlane \leq \maxBitPlane(t_resolution)$.

Each data block contains the following data in encoded format:

- 15 1. For $t_bitPlane \geq 2$:
 - a. A list of the indices of all subband coefficients whose absolute value is in the range $[2^{t_bitPlane-1}, 2^{t_bitPlane})$.
 - b. The sign of all the coefficients of a.
 - c. For $t_bitPlane > 2$, an additional precision bit for any coefficient that
 20 belongs to the current bit plane or any higher bit plane.
2. For $t_bitPlane = 1$, which we call the "least significant bit plane":
 - a. A list of the indices of HL-subband and HH-subband coefficients whose absolute value belongs to the set $\{-1, 0, 1\}$.
 - b. A "zero flag" for each coefficient of a, which indicates if the coefficient
 25 is equal to zero or not.
 - c. The sign of all the coefficients of a, whose "zero flag" is false.
 - d. The LSB of the HL-subband and HH-subband coefficients that belong to higher bit plane.

Remark:

30 Since the LH-subband contains only even coefficients, their LSB must be zero and is not coded.

3. For $t_bitPlane = 0$, which we call the "half bit plane", a matrix of

$\left(\frac{tileLength}{2}\right)^2$ bits associated with HH-subband coefficients as their last "half
 bit" (See (3.24) or (3.30)).

5. THE PROGRESSIVE SUBBAND CODING ALGORITHM

5.1 The encoding algorithm

The encoding algorithm of the present invention is performed at the server 120. In the present imaging system this rather time consuming task is performed locally in near real-time for a ROI, and not on the full image. The encoding algorithm is described for images with a single color component, such as grayscale images, but of course may also be applied to images with multiple color components. The straightforward generalization for an arbitrary number of components will be explained later.

The lossless algorithm receive as input the following parameters:

Variable	Meaning
<i>coef</i>	Matrix of subband coefficients, containing $3 \times \left(\frac{tileLength}{2} \right)^2$ coefficients
<i>HalfBit</i>	Matrix of bits containing $\left(\frac{tileLength}{2} \right)^2$ bits.

Table 4 - Lossless Encoding Algorithm Input Parameters

The coding strategy is similar in some sense to that described in A. Said and W. Pearlman, "A new, fast and efficient image codec based on set partitioning", IEEE Trans. Circuits and Systems for video Tech., Vol. 6, No. 3, pp. 243-250, 1996, but the preferred embodiment uses no "Zero Tree" data. For all the data blocks with $t_bitPlane \geq 2$, we use the lossy encoding algorithm described in previous art with the parameters:

- $coef := coef$ (The lossy parameter *coef* initialized with the lossless parameter *coef*)
- $equalBinSize := True$

- 5 • $\varepsilon_c := 2$

Remark: The lossy algorithm encodes all the bit-plane information for
 $t_bitPlane \geq 2$.

For $t_bitPlane \leq 1$, i.e. the least significant bit plane (of the lossless algorithm) and the
 10 half bit plane, we use a different algorithm described in 5.1.3.

5.1.1 Encoding algorithm initialization

The lossless encoding algorithm initialization is the same as the lossy algorithm
 of § 4.1.1 in the above-cited Ser. No. 09/386,264, which disclosure is incorporated
 15 herein by reference. In order to initialize the encoding algorithm, the following
 procedure is performed:

1. Assign to each coefficient $coef(x, y)$ its bit plane $b(x, y)$ such that:

$$|coef(x, y)| \in [\varepsilon_c 2^b, \varepsilon_c 2^{b+1})$$

20

2. Compute the maximum bit plane over all such coefficients:

$$maxBitPlane(tile) = \max_{x,y} (b(x, y))$$

- 25 3. Write the value of $maxBitPlane(tile)$ using one byte as the header of
 the data block:

$$(t_x, t_y, t_resolution, maxBitPlane(t_resolution))$$

4. Initialize all the coefficients as members of their corresponding *Type16*
 30 group.

5. Initialize a list of significant coefficients to be empty.

- 5 6. Initialize a coefficient approximation matrix *coef* as zero.

5.1.2 The outer loop

The outer loop of the encoding algorithm scans the bit planes from
 $b = \text{maxBitPlane}(\text{tile})$ to $b = 0$. The output of each such bit plane scan is the subband
 10 data block. Since the last stage of the encoding algorithm is arithmetic encoding of
 given symbols, at the beginning of each scan the arithmetic encoding output module is
 redirected to the storage area allocated for the particular data block. Once the bit plane
 scan is finished and the data block has been encoded, the output stream is closed and
 the bit plane b is decremented. After the outer loop is finished the following stages are
 15 performed:

1. Least significant bit plane is encoded ($t_bitPlane = 1$).
2. Half bit plane is encoded ($t_bitPlane = 0$).

20 The output of the least significant bit plane scan is the data block (Figure 14):

($t_x, t_y, t_resolution, t_bitPlane=1$).

The half bit plane data block is:

($t_x, t_y, t_resolution, t_bitPlane=0$).

25

5.1.3 Bit-plane scan

For $t_bitPlane \geq 2$, the framework of the bit plane scan is described in Figure
 24, while the pseudo code is given in the above-cited Ser. No. 09/386,264, which
 30 disclosure is incorporated herein by reference. The scan, for a given level b ($b \geq 2$),
 encodes all of the coefficients' data corresponding to the absolute value interval
 $[2^{b-1}, 2^b)$.

Remark: The encoder method `isLastBitPlane()` is associated to the $t_bitPlane = 2$.
 35

5 For the least significant bit plane, a pseudo code is described in Figure 15, while a flow chart is described in Figure 22.

Explanations to the least significant bit encoding algorithm:

1. The coefficients scanning procedure, i.e. moreCoef() procedure in Figure 15 or
"More coefficients?" in Figure 22 includes all the coefficients belong to the HH and
10 the HL-subband (Figure 14). The LH-subband is skipped, since the least significant
bit of each coefficient in it is zero (see remark 2 for (3.22)).
2. The procedure isCoefReported() ("Is coefficient reported?" in the flow chart)
returns false if the coefficient is one of $\{-1, 0, 1\}$, i.e. in all higher bit plane scans it
was insignificant, otherwise it returns true.
- 15 3. The procedure isCoefExactZero() ("Coefficient is zero?" in the flow chart) returns
true iff the coefficient is zero.
4. The procedure getCoefSign() returns the coefficient's sign.

For the half bit plane, a pseudo code is described in Figure 16.

20

5.2 The decoding algorithm

Obviously, this algorithm is a reversed step of the encoding algorithm of section
25 5.1, performed in the server 120. The client computer 110 during the progressive
rendering operation performs the decoding algorithm. Similar to the encoding
algorithm, the decoding algorithm is described for an image with one component (such
as a grayscale image), but of course could also be used with an image with more than
one component. The input parameters to the lossless algorithm are given below:

30

Variable	Meaning
<i>coef</i>	Empty matrix of subband coefficients to be filled by the decoding algorithm.
<i>HalfBit</i>	Matrix of bits containing $\left(\frac{tileLength}{2}\right)^2$ bits.

5

Table 5 - Lossless decoding algorithm input parameters

For all the data blocks with $t_bitPlane \geq 2$, a "lossy" decoding algorithm is utilized. The input parameters for the lossy algorithm are:

- 10
- $coef := coef$
 - $equalBinSize := True$
 - $\varepsilon_c := 2$

5.2.1 Decoding algorithm initialization

- 15
1. Assign to each coefficient $Coef(x, y)$ the value zero.
 2. Assign to each bit belongs to the HalfBit matrix the value zero.
 3. Initialize all the coefficients as members of their corresponding *Type16* group.
 4. Initialize the list of significant coefficients to be empty.
 5. If the "first" data block

20 $(t_x, t_y, t_resolution, maxBitPlane(t_resolution))$

is available at the client, read the first byte, which is the value of $maxBitPlane(tile)$.

5.2.2 The outer loop

Upon the completion of the outer loop in 5.1.2 the following stages are preformed:

- 25
1. The decoding algorithm scans the least significant bit plane. The input to this stage is encoded data block $(t_x, t_y, t_resolution, LeastSignificant_bitPlane)$.
 2. The decoding algorithm scans the half bit plane. The input to this stage is encoded data block $(t_x, t_y, t_resolution, Half_bitPlane)$.

5 5.2.3 Bit plane scan

The preferred embodiment follows the lossy prior art of the above-cited Ser. No. 09/386,264, which disclosure is incorporated herein by reference, for $t_bitPlane \geq 2$. The scan, for a given level b , decodes all of the coefficients' data corresponding to the absolute value interval $[\varepsilon 2^b, \varepsilon 2^{b+1})$. Pseudo codes of the least significant bit plane scan and half bit plane scan are described in Figure 16.

Explanations to the pseudo code:

1. The decoder's method **moreCoef()** scans all the coefficients in the HH, HL and LH subband. But, since the LH-subband is skipped in the encoding algorithm, we don't call to **decodeSymbol()** for its coefficients. Instead of this, we update their least significant bit as zero.
2. Recall that LH-subband coefficients that have not been reported until the least significant bit-plane must be zero since they are known to be even.

20

6. CLIENT WORKFLOW

With reference to Figure 4, we describe the workflow at the client unit 110. Any new ROI generated by the user's action such as a zoom-in, a scroll, or a luminance tuning invokes in step 401 a call from the GUI interface to the client imaging module with the new ROI view parameters. The client imaging module then computes in step 402 which data blocks are required for the rendering of the ROI and checks if these data blocks are available in the client cache. If not, their coordinate is added to a request list ordered according to some progressive mode. The request list is then encoded in step 403 and sent to the server. The server responds to the request by sending back to the client a stream of data blocks, in the order in which they were requested. In step 404 the client inserts them to their appropriate location in the distributed database. At various points in time step 405, a rendering of the ROI, is invoked. Naturally, the rendering operation is progressive and is able to use only the currently available data in the client's database.

35

5 6.1 Step 401:Receiving the ROI Parameters

The imaging module on the client computer 120 receives from the GUI interface module view parameters detailed in Table 5. These parameters are used to generate a request list for the ROI. The same parameters are used to render the ROI.

10

Table 5

Variable	Meaning
<i>worldPolygon</i>	A 2D polygon in the original image coordinate system
<i>scale</i>	The view resolution. $0 < scale < 1$ implies a low view resolution, $scale = 1$ original resolution and $scale > 1$ a higher than original view resolution
<i>deviceDepth</i>	A number in the set $\{8, 16, 24\}$ representing the depth of the output device (screen, printer)
<i>viewQuality</i>	A quality factor in the range $[1, 7]$ where 1 implies very low quality and 7 implies lossless quality
<i>luminanceMap</i>	If active: a curve defining a mapping of medical images with more than 8 bits (typically 10,12,16 bits) per grayscale values to an 8 bit screen
<i>progressiveMo</i>	One of: Progressive By Accuracy, Progressive By Resolution, Progressive by Spatial Order

15

The basic parameters of a ROI are *worldPolygon* and *scale* which determine uniquely the ROI view. If the ROI is to be rendered onto a viewing device with limited resolution, then a *worldPolygon* containing a large portion of the image will be coupled by a small *scale*. In the case where the rendering is done by a printer, the ROI could be a strip of a proof resolution of the original image that has arrived from the server computer 120. This strip is rendered in parallel to the transmission, such that the printing process will terminate with the end of transmission. The other view parameters determine the way in which the view will be rendered. The parameters *deviceDepth* and *viewQuality* determine the quality of the rendering operation. In

25

- 5 cases the viewing device is of low resolution or the user sets the quality parameter to a lower quality, the transfer size can be reduced significantly.

The parameter *luminanceMap* is typically used in medical imaging for grayscale images that are of higher resolution than the viewing device. Typically, 10 screens display grayscale images using 8 bits, while medical images sometimes represent each pixel using 16 bits. Thus, it is necessary to map the bigger pixel range to the smaller range of $[0, 255]$.

Lastly, the parameter *progressiveMode* determines the order in which data blocks should be transmitted from the server 120. The "Progressive By Accuracy" 15 mode is the best mode for viewing in low bandwidth environments. "Progressive By Resolution" mode is easier to implement since it does not require the more sophisticated accuracy (bit plane) management and therefore is commonly found in other systems. The superiority of the "progressive by accuracy" mode can be mathematically proven by showing the superiority of "non-linear approximation" over 20 "linear approximation" for the class of real-life images. See, e.g., R. A. DeVore, "Nonlinear approximation", Acta Numerica, pp. 51-150, 1998.

The "Progressive by Spatial Order" mode is designed, for example, for a "print on demand" feature where the ROI is actually a low resolution "proof print" of a high resolution graphic art work. In this mode the image data is ordered and received in a 25 top to bottom order, such that printing can be done in parallel to the transmission.

However, since lossless compression is mostly required in medical images transmission, where typically more than 8 bits images are used, we amplify our discussion on the curve (*luminanceMap* hereinabove) which defines the mapping from the original image gray scale range (typically 10,12,16 bits) to an 8-bit screen. Further 30 more, in medical images viewing, regardless of the original image depth, mapping is required in order to control the brightness and contrast of the image.

6.1.1 Luminance mapping

Mapping from original image depth (e.g. 10,12,16 bits) to screen depth 35 (typically 8-bits), is defined by a monotonic function (Figure 17):

$$f : [0, 2^{\text{original_image_depth}} - 1] \rightarrow [0, 2^{\text{screen_depth}} - 1]. \quad (6.1)$$

The curve influences not only the mapping, i.e. the drawing to the screen, but also the request from the server. To understand that, let us concentrate in the maximal gradient of the curve (Figure 17). In a lossy mode, the request is created such that the image approximation in the client side is close enough to the original image, i.e., the RMS (Root Mean Square Error) is visually negligible. When a curve (mapping function) is applied, the RMS can be increased or reduced. The maximal RMS increasing factor depends on the maximal gradient of the curve as follows:

$$\text{RMS_increasing_factor} = \frac{\text{RMS}(f(I), f(\hat{I}))}{\text{RMS}(I, \hat{I})} \leq \max(f'), \quad (6.2)$$

where

- I is the original image
- \hat{I} is the approximated image
- f is the mapping function
- $\text{RMS}(I_1, I_2) = \frac{\|I_1 - I_2\|_{L_2}}{\text{Image_size}}$
- $\max(f')$ is the maximal gradient of the curve.

We consider the worst case of the RMS increasing factor i.e.:

$$\text{RMS_increasing_factor} = \text{Maximal_gradient} = \max(f')$$

If the RMS increasing factor is greater than 1, it means that the “new RMS” may be greater than we consider as visually negligible error. Thus, the request list should be increase (more bit-planes should be requested from the server) in order to improve the approximation accuracy. Conversely, if the RMS increasing factor is smaller than 1, the request listing can be reduced. The exact specification of this is given in the following section.

30

6.2 Step 402: Creating the request list

In step 402 using the ROI view parameters, the client imaging module at the client computer 110 calculates data blocks request list ordered according to the *progressiveMode*. Given the parameters *worldPolygon* and *Scale*, it may be determined which subband tiles in the “frequency domain” participate in the

35

5 reconstruction of the ROI in the "time domain". These tiles contain all the coefficients that are required for an "Inverse Subband/Wavelet Transform" (IWT) step that produces the ROI. First, the parameter $dyadicResolution(ROI)$ is computed, which is the lowest possible dyadic resolution higher than the resolution of the ROI. Any subband tiles of a higher resolution than $dyadicResolution(ROI)$ do not participate in

10 the rendering operation. Their associated data blocks are therefore not requested, since they are visually insignificant for the rendering of the ROI. If $scale \geq 1$, then the highest resolution subband tiles are required. If $scale \leq 2^{1-numberOfResolutions}$ then only the lowest resolution tile is required. For any other value of $scale$ we perform the mapping described below in Table 6.

15

Table 6

<i>scale</i>	<i>highestSubbandResolution</i>
$scale \leq 2^{1-numberOfResolutions}$	1
$2^{1-numberOfResolutions} < scale \leq 1$	$numberOfResolutions - \lfloor -\log_2(scale) \rfloor$
$scale > 1$	$numberOfResolutions$

20 Once it has been determined which subband tiles participate in the rendering of the ROI, it is necessary to find which of their data blocks are visually significant and in what order they should be requested. Using well known rate/distortion rules from the field of image coding (such as is described in S. Mallat and F. Falzon, "Understanding image transform codes", Proc. SPIE Aerospace Conf., 1997), it is not too difficult to

25 determine an optimal order in which the data blocks should be ordered by the client imaging module (and thus delivered by the server 120). This optimal order is described in steps 301-310 of Figure 3 for the "Progressive By Accuracy" mode. The underlying mathematical principal behind this approach is "Non-Linear Approximation".

30 First, the subband coefficients with largest absolute values are requested since they represent the most visually significant data such as strong edges in the image. Notice that high resolution coefficients with large absolute value are requested before low resolution coefficients with smaller absolute value. Within each given layer of precision (bit plane) the order of request is according to resolution; low resolution

- 5 coefficients are requested first and the coefficients of *highestSubbandResolution* are requested last.

The main difficulty of this step is this: Assume a subband tile is required for the rendering of the ROI. This means that $t_resolution \leq dyadicResolution(ROI)$ and the tile is required in the IWT procedure that reconstructs the ROI. It must be understood
 10 which of the data blocks associated with the subband tile represent visually insignificant data and thus should not be requested. Sending all of the associated data blocks will not affect the quality of the progressive rendering. However, in many cases transmitting the "tail" of data blocks associated with high precision is unnecessary since it will be visually insignificant. In such a case, the user will see that the
 15 transmission of the ROI from the server 120 is still in progress, yet the progressive rendering of the ROI seems to no longer to change the displayed image.

Additionally, the influence of the luminance mapping on the accuracy level of the requested data block as described below. Supposing for some t_x, t_y and $t_resolution$, the set

$$20 \quad \{(t_x, t_y, t_resolution, t_bitPlane) | T \leq t_bitPlane \leq maxPlaneBit(t_resolution)\}$$

is requested where T is the minimal bit plane required to the current view. Here, where the luminance mapping is taken in account, the value of T might be increased or decreased.

- 25 The number of bit planes reduced (added) from the request list is

$$\left\lfloor \log_2 \left(\frac{1}{Maximal_gradient} \right) \right\rfloor.$$

I.e., for those t_x, t_y and $t_resolution$ mentioned before, the following set is requested:

$$\{(t_x, t_y, t_resolution, t_bitPlane) | T' \leq t_bitPlane \leq maxPlaneBit(t_resolution)\}$$

- 30 where

$$T' = T + \left\lfloor \log_2 \left(\frac{1}{Maximal_gradient} \right) \right\rfloor.$$

Examples:

5 1. Given

- Image depth of 12-bit
- Screen depth of 8-bit
- Linear luminance mapping, I.e., $Maximal\ gradient = \frac{2^8}{2^{12}} = 2^{-4}$.

The number of bit planes reduced from the request list is:

$$10 \quad \left\lfloor \log_2 \left(\frac{1}{Maximal\ gradient} \right) \right\rfloor = \left\lfloor \log_2 \left(\frac{1}{2^{-4}} \right) \right\rfloor = 4.$$

2. Given a luminance mapping with $Maximal\ gradient = 2$

The number of bit planes reduced from the request list is:

$$\left\lfloor \log_2 \left(\frac{1}{Maximal\ gradient} \right) \right\rfloor = \left\lfloor \log_2 \left(\frac{1}{2} \right) \right\rfloor = -1.$$

Thus one bit plane is added to the original set.

15

6.3 Step 403: Encoding the request list

The client imaging module in the client computer 110 encodes the request list into a request stream that is sent to the server computer 120 via the communication network 130 (Figure 1). The request list encoding algorithm is a simple rectangle-based procedure. The heuristics of the algorithm is that the requested data block usually can be grouped into data block rectangles. From the request list of data blocks indexed by the encoding algorithm computes structures of the type

$$25 \quad \{(t_x, t_y, t_resolution, t_bitPlane), n_x, n_y\}, \quad n_x, n_y \geq 1$$

(1.3)

Each such structure represents the $n_x \times n_y$ data blocks

$$\{(t_x + i, t_y + j, t_resolution, t_bitPlane)\}, \quad 0 \leq i < n_x, 0 \leq j < n_y,$$

30

5 The encoding algorithm attempts to create the shortest possible list of structures, collecting the data blocks to the largest possible rectangles can do this. It is important to note that the algorithm ensures the order of data blocks in the request list is not changed, since the server 120 will respond to the request stream by transmitting data blocks in the order in which they were requested. A good example of when this works
 10 well is when a user zooms in into a ROI at a high resolution that was never viewed before. In such a case the request list might be composed of hundreds of requested data blocks, but they will be collected to one (x, y) rectangle for each pair $(t_resolution, t_bitPlane)$.

15

6.4 Step 404: Receiving the data blocks

The client computer 110 upon receiving from the server computer 120 an encoded stream containing data blocks, decodes the stream and inserts the data blocks into their appropriate location in the distributed database using their ID as a key. The
 20 simple decoding algorithm performed here is a reversed step of the encoding infra. Since the client 110 is aware of the order of the data blocks in the encoded stream, only the size of each data block need be reported along with the actual data. In case the server 120 informs of an empty data block, the receiving module marks the appropriate slot in the database as existing but empty.

25 Recall that the subband tile associated with each data block is denoted by the first three coordinates of the four coordinates of a data block $(t_x, t_y, t_resolution)$. From the subband tile's coordinates the dimensions are calculated of the area of visual significance; that is, the portion of the ROI that is affected by the subband tile. Assume that each subband tile is of length *tileLength* and that the wavelet basis used has a
 30 maximal filter size *maxFilterSize*, then defining $hFilterSize = \lceil maxFilterSize/2 \rceil$ and $factor := numberOfResolutions - t_resolution + 1$, we have that the dimensions of the affected region of the ROI (in the original image's coordinate system) are

$$5 \quad \begin{bmatrix} t_x \times \text{tileLength}^{\text{factor}} - h\text{FilterSize}^{\text{factor}}, (t_x + 1) \times \text{tileLength}^{\text{factor}} + h\text{FilterSize}^{\text{factor}} \end{bmatrix} \times \\ \begin{bmatrix} t_y \times \text{tileLength}^{\text{factor}} - h\text{FilterSize}^{\text{factor}}, (t_y + 1) \times \text{tileLength}^{\text{factor}} + h\text{FilterSize}^{\text{factor}} \end{bmatrix}$$

These dimensions are merged into the next rendering operation's region. The rendering region is used to efficiently render only the updated portion of the ROI.

10

6.5 Progressive Rendering

During the transmission of ROI data from the server to the client, the client performs rendering operations of the ROI. To ensure that these rendering tasks do not interrupt the transfer, the client runs two program threads: communications and
15 rendering. The rendering thread runs in the background and draws into a pre-allocated "off-screen" buffer. Only then does the client use device and system dependant tools to output the visual information from the "off-screen" to the rendering device such as the screen or printer.

The rendering algorithm performs reconstruction of the ROI at the highest
20 possible quality based on the available data at the client. That is, data that was previously cached or data that "just" arrived from the server. For efficiency, the progressive rendering is performed only for the portion of the ROI that is affected by newly arrived data. Specifically, data that arrived after the previous rendering task began. This "updated region" is obtained using the method of step 404 described in
25 §6.4.

The parameters of the rendering algorithm are composed of two sets:

1. The ROI parameters described in Table 3.
2. The parameters transmitted from the server explained in Table 5 , with the
30 exception of the *jumpSize* parameter, which is a "server only" parameter.

The rendering algorithm computes pixels at the dyadic resolution *dyadicRresolution(ROI)*. Recall that this is the lowest possible dyadic resolution that is higher than the resolution of the ROI. The obtained image is then resized to the correct

5 resolution. Using a tiling of the multiresolution representation of the ROI, the steps of the algorithm are performed on a tile by tile basis as described in Figure 11. Since the tiles' length are *tileLength*, which is typically chosen as 64, the rendering algorithm is memory efficient.

10 6.5.1 The rendering rate

As ROI data is transmitted to the client 110, the rendering algorithm is performed at certain time intervals of a few seconds. At each point in time, only one rendering task is performed for any given displayed image. To ensure that progressive rendering does not become a bottleneck, two rates are measured: the data block transfer rate and the ROI rendering speed. If it predicted that the transfer will be finished before a rendering task, a small delay is inserted, such that rendering will be performed after all the data arrives. Therefore, in a slow network scenario (as the Internet often is), for almost the entire progressive rendering tasks, no delay is inserted. With the arrival of every few kilobytes of data, containing the information of a few data blocks, a rendering task visualizes the ROI at the best possible quality. In such a case the user is aware that the bottleneck of the ROI rendering is the slow network and has the option to accept the current rendering as a good enough approximation of the image and not wait for all the data to arrive.

25 6.5.2 Memory constraint subband data structure

This data-structure is required to efficiently store subband coefficients, in memory, during the rendering algorithm. This is required since the coefficients are represented in long integer (lossless coding mode) or floating-point (lossy coding mode) precision which typically require more memory than pixel representation (1 byte). In lossy mode, the coefficients at the client side 110 are represented using floating-point representation, even if they were computed at the server side 120 using an integer implementation. This will minimize round-off errors.

At the beginning of the rendering algorithm, coefficient and pixel memory strips are initialized. *dyadicWidth(ROI)* may be denoted as the width of the projection of the

- 5 ROI onto the resolution $dyadicResolution(ROI)$. For each component and resolution $1 < j \leq dyadicResolution(ROI)$, four subband strips are allocated for the four types of subband coefficients: hl, lh, hh and HalfBit. The coefficient strips are allocated with dimensions

$$10 \quad \left[2^{j-dyadicResolution(ROI)-1} \times dyadicWidth(ROI), \frac{3}{2} \times tileLength + \frac{maxFilterSize}{2} \right]$$

For each component and resolution $1 \leq j < dyadicResolution$ a pixel strip is allocated with dimensions

$$15 \quad \left[2^{j-dyadicResolution(ROI)} \times dyadicWidth(ROI), tileLength + \frac{maxFilterSize}{2} \right]$$

- Beginning with the lowest resolution 1, the algorithm proceeds with a recursive multiresolution march from the top of the ROI to bottom (y direction. Referring to Figures 10 and 11, in step 1101, the multiresolution strips are filled with sub-tiles of coefficients 1050 decoded from the database or read from the memory cache. From the coefficients we obtain multiresolution pixels 1051 using an inverse subband transform step 1102 (shown in further detail in Figure 10). Each time a tile of pixels at resolutions $j < dyadicResolution(ROI)$ is reconstructed, it is written into the pixel strip at the resolution j . Each time a tile of pixels at the highest resolution $dyadicResolution(ROI)$ is reconstructed, it is fed into the inverse color transform and resizing steps 1103, 1104.

6.5.3 Step 1101: decoding and memory caching

- The subband coefficients data structure described previously in section 6.5.2 is filled on a tile basis. Each such subband tile is obtained by decoding the corresponding data blocks stored in the database or reading from the memory cache. The memory cache is used to store coefficients in a simple encoded format. The motivation is this: the decoding algorithm described previously in section 5.2 is computationally intensive

5 and thus should be avoided whenever possible. To this end the rendering module uses a memory cache 111 where subband coefficient are stored in very simple encoded format which decodes very fast. For each required subband tile, the following extraction procedure is performed, described in Figure 25, beginning at step2501. In step2502, if no data blocks are available in the database for the subband tile, its coefficients are set to zero (step2503). In step2504, if the tile's memory cache storage is updated, namely it stores coefficients in the same precision as in the database, then the coefficients can be efficiently read from there (step2505). In step2506, the last possibility is that the database holds the subband tile in higher precision. Then, the tile is decoded down to the lowest available bit plane using the algorithm previously described in section 5.2 and the cached representation is replaced with a representation of this higher precision information.

6.5.4 Step 1102: inverse lossless wavelet transform

This is an inverse step to step 603 performed in the server (see 7.1.5). Following Figure 21 we see that four "extended" subband coefficient sub-tiles of length $tileLength/2 + maxFilterSize$ at the resolution i are read from the coefficient strips data structure and transformed to a tile of pixels at the next higher resolution using $losslessWaveletdTransformType(i)$. If $i+1 < dyadicResolution(ROI)$, the tile of pixels obtained by this step is inserted into the pixel memory strip at the resolution $i+1$. If $i+1 = dyadicResolution(ROI)$ the tile of pixels is processed by the next step of color transform.

Remark: Recall from 5.1.1 that the "half bits" are initialized as zeros, therefore the inverse step is well defined even if their "real" value is not available in the client yet.

30 6.5.5 Step 1103: inverse color transform

This is an inverse step to step 603 performed at the server 120. It is performed only for tiles of pixels at the resolution *highestSubbandResolution*. At this stage, all of the pixels of each such tile are in the *outputColorSpace* and so need to be transformed into a displaying or printing color space. For example, if the original image at the server 120 is a color image in the color space RGB, the pixels obtained by the previous

5 step of inverse subband transform are in the compression color space YUV. To convert back from YUV to RGB, we use the inverse step described in Figure 13. If the ROI is at an exact dyadic resolution, then the tile of pixels in the rendering color space is written into the off-screen buffer. Else it is resized in the next step.

10

6.5.6 Step 1104: image resize

In case the resolution of the ROI is not an exact dyadic resolution, the image obtained by the previous step must be re-sized to this resolution. This can be accomplished using operating system imaging functionality. In most cases the
15 operating system's implementation is sub-sampling which produces in many cases an aliasing effect which is visually not pleasing. To provide higher visual quality, the imaging system of the present invention may use the method of linear interpolation, for example described in J. Proakis and D. Manolakis, "Digital signal processing", Prentice Hall, 1996. The output of the interpolation is written to the off-screen buffer. From
20 there it is displayed on the screen using system device dependant methods.

6.5.7 Step 1105: mapping to 8-bit screen

When *luminanceMap* is active mapping to 8-bit screen is performed using the mapping function described in 6.1.1.

25

7. SERVER WORKFLOW

With reference to Figure 5, the operation of the server computer 120 (Figure 1) will now be described. Initially, an uncompressed digital image is stored in, for example, storage 122 of the server computer 120. This uncompressed digital image
30 may be a two-dimensional image, stored with a selected resolution and depth. For example, in the medical field, the uncompressed digital image may be contained in a DICOM file.

Once the client computer 110 requests to view or print a certain image, the server performs the preprocessing step 501. This step is a computation done on data
35 read from the original digital image. The results of the computation are stored in the

5 server cache device 121. After this fast computation a "ready to serve" message is sent from the server to the client containing basic information on the image.

In step 502, the server receives an encoded stream of requests for data blocks associated with a ROI that needs to be rendered at the client. The server then decodes the request stream and extracts the request list.

10 In step 503, the server reads from cache or encodes data block associated with low resolution portions of the ROI, using the cached result of the preprocessing stage 501.

If the ROI is a high-resolution portion of the image, the server, in step 504, reads from cache or performs a "local" and efficient version of the preprocessing step 501. Specifically, a local portion of the uncompressed image, associated with the ROI, is read from the storage 122, processed and encoded. In step 505, the data that was encoded in steps 503-504 is progressively sent to the client in the order it was requested.

20 **7.1 Step 501: preprocessing**

The preprocessing step is now described with respect to Figure 6. The preprocessing algorithm's goal is to provide the fastest response to the user's request to interact with the image. Once this fast computational step is performed, the server is able to provide efficient "pixel-on-demand" transmission of any client ROI requests that will follow. In most cases the first ROI is a view of the full image at the highest resolution that "fits" the viewing device. The preprocessing algorithm begins with a request for an uncompressed image that has not been processed before or has been processed but the result of this previous computation has been deleted from the cache. As explained, this unique algorithm replaces the possibly simpler procedure of encoding the full image into some progressive format. This latter technique will provide a much slower response to the user's initial request than the technique described below. At the end of the algorithm a "ready to serve ROI of the image" message is sent to the client containing basic information on the image. While some of this information, image dimensions, original color space, resolution etc., is available to the user of the client computer, most of this information is "internal" and required by

- 5 the client to formulate ROI request lists (§6.2) and progressively render (§6.5). Next we describe in detail the preprocessing algorithm.

7.1.1 Preprocessing Parameters

Table 7

10

Variable	Meaning
<i>losslessMode</i>	If true, preprocessing will prepare data that can be used for lossless transmission.
<i>subbandTransformType</i>	The framework allows the ability to select a different subband transform for each resolution of each image. The technical term is: non-stationary transforms.
<i>numberOfResolutions</i>	The number of resolutions in the Multiresolution structure calculated for the image. Typically, $numberOfResolutions = \log_2(\sqrt{ImageSize})$.
<i>jumpSize</i>	A number in the range $[0, numberOfResolutions - 1]$. The preprocessing stage computes only the top lower part of the image's multiresolution pyramid of the size $numberOfResolutions - jumpSize$.
<i>tileLength</i>	Typically = 64. Tradeoff between time and coding performance.
$nTilesX(j)$	Number of subband tiles in the x direction at the resolution j
$nTilesY(j)$	Number of subband tiles in the y direction at the resolution j
<i>inputColorSpace</i>	Color space of uncompressed original image.
<i>outputColorSpace</i>	Transmitted color space used as part of the encoding technique.
<i>numberOfComponents</i>	Number of components in <i>OutputColorSpace</i> .
$threshold(c, j)$	A matrix of values used in lossy compression. The subband coefficients of the component c at the resolution j with absolute value below $threshold(c, j)$ are considered as (visually) insignificant and set to zero.

Given an input image, the parameters described in Table 7 are computed or chosen. These parameters are also written into a header sent to the client 110 and are

5 used during the progressive rendering step 405 (see section 6.5, described previously).
The important parameters to select are:

1. *losslessMode*: In this mode, progressive transmission of images takes place until lossless quality is obtained. Choosing this mode requires the preprocessing algorithm to use certain reversible wavelet transforms, and can slow down the algorithm.
2. *subbandTransformType(j)*: The (dynamic) selection of wavelet basis (as described, for example, in I. Daubechies, "Ten lectures on wavelets", Siam, 1992) is crucial to the performance of the imaging system. The selection can be non-stationary, meaning a different transform for each resolution j . The selection is derived from the following considerations:
 - a. Coding performance (in a rate/distortion sense): This is obviously required from any decent subband/wavelet transform.
 - b. Approximation of ideal low pass: It is favorable to choose a transform such that low resolutions of the image will be of high visual quality (some filters produce poor quality low resolutions even before any compression takes place).
 - c. Fast transform implementation: Can the associated fast transform be implemented using lifting steps (as described, for example, by I. Daubechies and W. Sweldens, "Factoring wavelet transforms into lifting steps", J. Fourier Anal. Appl., Vol. 4, No. 3, pp. 247-269, 1998), using only integer shifts and additions, etc. Some good examples are the Haar and CDF transforms (1,3), (2,2)*** described in I. Daubechies, "Ten lectures on wavelets", Siam, 1992.
 - d. Fast low pass implementation: A very important parameter, since together with the parameter *jumpSize*, it determines almost all of the complexity of the algorithm. For example, the

- 5 CDF (1,3) is in this respect the "optimal" transform with three
vanishing moments. Since the dual scaling function is the simple
B-spline of order 1, its low pass is simple averaging. Thus, the
sequence of CDF transforms, using the B-spline of order 1 as the
10 dual scaling function, but with wavelets with increasing number
of vanishing moments are in some sense optimal in the present
system. They provide a framework for both real time response
and good coding efficiency.
- e. Lossless mode: If *losslessMode* is true we must choose the
filters from a subclass of reversible transforms (see, for example,
15 "Wavelet transforms that map integers to integers", A.
Calderbank, I. Daubechies, W. Sweldens, B. L. Yeo, J. Fourier
Anal. Appl., 1998).
- f. Low system I/O: If the network 130 in Figure 1 connecting
between the Image residing on the storage 122 and the imaging
20 server 120 is slow, the bottleneck of the preprocessing stage (and
the whole imaging system for that fact) might be simply the
reading of the original image. In such a case a transform may be
chosen with a lazy sub-sampling low pass filter that corresponds
to efficient selective reading of the input image. Many
25 interpolating subband transforms with increasing number of
vanishing moments can be selected to suit this requirement.
However, this choice should be avoided whenever possible, since
it conflicts with (a) and (b).
- g. Image type: If the type of the image is known in advance, an
30 appropriate transform can be chosen to increase coding
efficiency. For example: Haar wavelet for graphic images,
smoother wavelet for real-life images, etc. In the graphic arts
field, there are numerous cases of documents composed of low
resolution real-life images and high resolution graphic content.
35 In such a case, a non-stationary sequence of transforms may be
chosen: Haar for the high resolutions and a smoother basis

5 starting at the highest resolution of a real-life image part. In case of low system I/O (f), a non-stationary choice of interpolating transforms of different orders is required.

- 10 3. *jumpSize*: This parameter controls the tradeoff between fast response to the user's initial request to interact with the image and response times to subsequent ROI requests. When *jumpSize* is large, the initial response is faster, but each computation of a region of interest with higher resolution than the jump might require processing of a large portion of the original image.
- 15 4. *InputColorSpace*: The input color spaces supported in lossless mode are:
- a. Grayscale: For grayscale images
 - b. RGB
- 20 5. *outputColorSpace*: The following are color spaces which perform well in coding:
- a. Grayscale: For grayscale images
 - b. YUV: for viewing color images

Referring to Table 7 [LP], *losslessMode* is set to true. *Threshold* (*c, j*) is not in use, since in lossless mode, there is no thresholding. The rest of the variables have the same meaning as in the lossy algorithm.

25

7.1.2 Memory constraint multiresolution scan data structure

30 Most wavelet coding algorithms have not addressed the problem of memory complexity. Usually the authors have assumed there is sufficient memory such that the image can be transformed in memory from the time domain to a wavelet frequency domain representation. It seems the upcoming JPEG2000 will address this issue, as did its predecessor JPEG. The preprocessing algorithm also requires performing subband

35 transforms on large images, although not always on the full image, and thus requires

5 careful memory management. This means that the memory usage of the algorithm is not of the order of magnitude of the original image, as described in J. M. Shapiro, "An embedded hierarchical image coder using zero-trees of wavelet coefficients", IEEE Trans. Sig. Proc., Vol. 41, No. 12, pp. 3445-3462, 1993.

10 Given an uncompressed image we allocate the following number of memory strips

$$\text{numberOfComponents} \times (\text{numberOfResolutions} - \text{jumpSize})$$

of sizes

15

$$\left[2^{-(\text{numberOfResolutions}-j)} \text{imageWidth}, 3 \times \text{tileLength} / 2 + \text{maxFilterSize} \right]$$

for $1 \leq j \leq \text{numberOfResolutions} - \text{jumpSize} - 1$ and

20

$$\left[\text{imageWidth}, \text{tileLength} + 2 \times \text{maxFilterSize} \right]$$

for $j = \text{numberOfResolutions} - \text{jumpSize}$

25 That is, the memory usage is proportional to $2^{-\text{jumpSize}} \times \text{imageWidth}$. Each such strip stores low-pass coefficients in the color space *outputColorSpace* at various resolutions.

Referring to Figure 6, during the preprocessing stage, the resolutions are scanned simultaneously from start to end in the *y* direction. For each color component and resolution, the corresponding strip stores low-pass coefficients or pixels at that resolution. The core of the preprocessing algorithm are steps 604-607, where tiles of
30 pixels of length $\text{tileLength} + 2 \times \text{maxFilterSize}$ are read from the memory strips and handled one at a time. In step 604 the tile is transformed into a tile of length tileLength containing two types of coefficient data: subband coefficients and pixels at a lower resolution. The subband coefficients are processed in steps 605-606 and are stored in

5 the cache. The lower resolution pixels are inserted in step 607 to a lower resolution memory strip. Whenever such a new sub-tile of lower resolution pixels is inserted into a strip, the algorithm's memory management module performs the following check: If the part of the sub-tile exceeds the current virtual boundaries of the strip, the corresponding first lines of the strip are considered unnecessary anymore. Their
 10 memory is (virtually) re-allocated for the purpose of storing the sub-tile's new data.

7.1.3 Step 601: Lossless color-transform

This step is uses the conversion formula described in Figure 13. This step must be performed before step 602, because the lossless color conversion is non-linear.

15

7.1.4 Step 602: Lossless Wavelet Low Pass

The motivation for the low pass step is explained in § 6.1.4 in the above-cited Ser. No. 09/386,264, which disclosure is incorporated herein by reference. In a lossless mode there are a few emphasis that are represented here.

20 In step 602, the low pass filters of the transforms $subbandTransformType(j)$,

$numberOfResolutions - jumpSize < j \leq numberOfResolutions$, are used to obtain a low resolution strip at the resolution $numberOfResolutions - jumpSize$ (as can be seen in Figure 26). Typically, it is required to low pass about $2^{jumpSize}$ lines of the original image 1010 to produce one line of the low resolution image. The low pass calculation is initiated by a read of tiles of pixels from the memory strips performed in step 604. Whenever there is an attempt to read missing low resolution lines, they are computed by low passing the original image and inserted into the memory strip. The insertion over-writes lines are no longer required, such that the algorithm is memory constrained.
 25
 30 In the case where a non-linear color transform took place in the previous step 601, the results of that transform are low-passed.

In the lossless mode of operation, the *jumpSize* parameter defines the number of lossless wavelet low pass steps should be done. A single low pass step is the same for Haar and CDF (1,3) and defined by the following two stages (taken from (3.20) and
 35 (3.22):

$$5 \quad \text{X-direction: } s(n) = \left\lfloor \frac{x(2n) + x(2n+1)}{2} \right\rfloor$$

$$\text{Y-direction: } s(n) = x(2n) + x(2n+1).$$

Namely, in a 2D representation, the low pass step is defined by

$$ll(m, n) = \left\lfloor \frac{x(2m+1, 2n+1) + x(2m, 2n+1)}{2} \right\rfloor + \left\lfloor \frac{x(2m+1, 2n) + x(2m, 2n)}{2} \right\rfloor. \quad (7.1)$$

10 For $jumpSize = 1$ and $jumpSize = 2$ (other sizes practically are not needed), the server performs these steps efficiently (almost like the lossy algorithm) by a single operation that simulates exactly $jumpSize$ low pass steps defined in (7.1). As noticed from (7.1), the simplicity of the formula makes filters such as Haar and CDF (1,3) "optimal" in the respect of low pass efficiency.

15

7.1.5 Step 603: Forward lossless Wavelet transform

In Step 603 we perform one step of an efficient local lossless wavelet transform (§3), on a tile of pixels at the resolution $1 \leq j \leq numberOfResolutions - jumpSize$. The type of transform is determined by the parameter $losslessWaveletTransformType(j)$.

20 As described in Figure 1, the transform is performed on an "extended" tile of pixels is of length $tileLength + 2 \times maxFilterSize$ (unless we are at the boundaries), read directly from a multi-resolution strip at the resolution $j+1$. The output of the step is a lossless subband tile composed of wavelet coefficients including Half bit coefficients and low resolution coefficients/pixels. The transform step is efficiently implemented in integers as described in §3.

25

The subband transform of step 603 outputs three types of data: scaling function (low pass), wavelet (high pass) and Halfbits. The wavelet coefficients are treated in step 604 while the scaling function coefficients are treated in step 605.

30 **Remark:** Tiles of pixels which are located on the boundaries sometimes need to be padded by extra rows and/or columns of pixels, such that they will formulate a "full" tile of length $tileLength$.

5 7.1.6 Step 604: Variable Length encoding and storage

In step 604, the subband coefficients that are calculated in step 603 are variable length encoded and stored in the cache 121. If $\text{maxBitPlane}(\text{tile}) = 0$ we do not write any data. Else we loop on the coefficient groups $\{\text{coef}(2 \times i + x, 2 \times j + y)\}_{x,y=0,1}$. For each such group we first write the group's variable length $\text{length}(i, j)$ using

10 $\log_2(\text{maxBitPlane}(\text{tile}))$ bits. Then for each coefficient in the group we write $\text{length}(i, j) + 1$ bits representing the coefficient's value. The least significant bit represents the coefficient's sign: if it is 1 then the variable length encoded coefficient is assumed to be negative. The HalfBit subband coefficients are written in one-bit per

15 coefficient.

7.1.7 Step 605: Copying low pass coefficients into the multiresolution strip structure

In step 503, unless *losslessMode* is true, the subband coefficients calculated in

20 step 604 are quantized. This procedure is performed at this time for the following reason: It is required that the coefficients computed in the previous step will be stored in the cache 121. To avoid writing huge amounts of data to the cache, some compression is required. Thus, the quantization step serves as a preparation step for the next variable length encoding step. It is important to point out that the quantization

25 step has no effect on compression results. Namely, the quantization step is synchronized with the encoding algorithm such that the results of the encoding algorithm of quantized and non-quantized coefficients are identical.

A tile of an image component c at the resolution j is quantized using the given threshold $\text{threshold}(c, j)$: for each coefficients x , the quantized value is

30 $\lfloor x / \text{threshold}(c, j) \rfloor$. It is advantageous to choose the parameters $\text{threshold}(c, j)$ to be dyadic such that the quantization can be implemented using integer shifts. The quantization procedure performed on a subband tile is as follows:

- 5 1. Initialize $\text{maxBitPlane}(\text{tile}) = 0$.
2. Loop over each group of four coefficients
 $\{coef(2 \times i + x, 2 \times j + y)\}_{x,y=0,1}$. For each such group initialize a variable
length parameter $\text{length}(i, j) = 0$.
- 10 3. Quantize each coefficient in the group $coef(2 \times i + x, 2 \times j + y)$ using the
appropriate threshold.
4. For each coefficient, update $\text{length}(i, j)$ by the bit plane b of the
15 coefficient, where the bit plane is defined by
$$|coef(2 \times i + x, 2 \times j + y)| \in [2^b \text{threshold}(c, j), 2^{b+1} \text{threshold}(c, j))$$
5. After processing the group of four coefficients, use the final value of
20 $\text{length}(i, j)$ to update $\text{maxBitPlane}(\text{tile})$ by
$$\text{maxBitPlane}(\text{tile}) = \max(\text{maxBitPlane}(\text{tile}), \text{length}(i, j))$$
6. At the end of the quantization step, store the value $\text{maxBitPlane}(\text{tile})$ in
25 the cache 121.

Note that for subband tiles located at the boundaries we can set to zero subband coefficients that are not associated with the actual image, but only with a padded portion. To do this we take into account the amount of padding and the parameter
30 maxFilterSize . The motivation for the "removal" of these coefficients is coding efficiency.

5 7.2 Step 502: Decoding the request stream

This is the inverse step of section 6.3. Once the request stream arrives at the server 120, it is decoded back to a data block request list. Each data structure the type representing a group of requested data blocks is converted to the sub-list of these data blocks.

10

7.3 Step 503: Encoding low resolution part of ROI

Step 503 is described in Figure 7. It is only performed whenever the data blocks associated with low-resolution subband tile are not available in the server cache 121.

15

Step 701 is the inverse step of step 604 described in §7.1.6. In the preprocessing algorithm subband tiles of lower resolution, that is resolutions lower than $numberOfResolutions - jumpSize$, were stored in the cache using a variable length type algorithm. For such a tile we first need to decode the variable length representation. The algorithm uses the stored value $maxBitPlane(tile)$.

20

1. If $maxBitPlane(tile) = 0$, then all the coefficients are set to zero including the HalfBit subband.
2. If $maxBitPlane(tile) = 1$, then all the coefficients are set to zero, and the HalfBit subband coefficient are read bit by bit from cache.
3. Else, as performed in 2, the HalfBit subband coefficient are read bit by bit from

25

cache, and we perform the following simple decoding algorithm:

For each group of four coefficients $\{coef(2 \times i + x, 2 \times j + y)\}_{x,y=0,1}$, we read $\log_2(maxBitPlane(tile))$ bits representing the variable length of the group.

Assume the variable length is $length(i, j)$. For each of the four coefficients we
 30 then read $length(i, j) + 1$ bits. The least significant bit represents the sign. The reconstructed coefficient takes the value:

$$5 \quad (readBits \gg 1) \times \begin{cases} -1 & readBits \& 1 = 1 \\ 1 & readBits \& 1 = 0 \end{cases}$$

In step 702 we use the encoding algorithm described in §5.1 to encode the requested data blocks associated with the extracted subband tile.

10 **7.4 Step 504: Processing high resolution part of ROI**

Step 504 is described in Figure 8. In case we have used *jumpSize* > 0 in step 501 and the resolution of the ROI > *numberOfResolutions* - *jumpSize*, we are sometimes required to perform a local variation of the preprocessing step described in §7.1.

Whenever the server receives a request list of data blocks we check the following. If a
 15 data block has been previously computed (present in the cache 121) or is associated with a low resolution subband tile data block then it is either simply read from the cache or handled in step 503. Else, the coordinates of the data block are used to find the "minimal" portion of the ROI that needs to be processed. Then, a local version of the preprocessing algorithm is performed for this local portion. The difference here is that
 20 step 804 replaces Variable Length coding step 604 of the preprocessing algorithm by the encoding algorithm given in §5.1.

7.5 Step 505: Progressive transmission of ROI

In the final step, the encoded data tiles are sent from the server 120 to the client
 25 110, in the order they were requested. In many cases, data blocks will be empty. For example, for a region of the original image with a constant pixel value, all of the corresponding data blocks will be empty, except for the first one that will contain only one byte with the value zero representing $maxBitPlane(tile) = 0$. For a low activity region of the image, only the last data blocks representing higher accuracy will contain
 30 any data. Therefore, to avoid the extra side information, rectangles of empty data blocks are collected and reported to the client 110 under the restriction that they are reported in the order in which they were requested. For blocks containing actual data, only the data block's size in bytes need be reported, since the client 110 already knows which data blocks to expect and in which order.

- 5 The present invention has been described in only a few embodiments, and with respect to only a few applications (e.g., commercial printing and medical imaging). Those of ordinary skill in the art will recognize that the teachings of the present invention may be used in a variety of other applications where images are to be transmitted over a communication media

What is claimed:

1. A system for transmitting a digital image over a communication network, comprising:

- (a) an image storage device for storing a digital image;
- (b) a client computer coupled to the communication network, wherein the client computer generates and transmits across the communication network coordinates defining a region of interest within the digital image;
- (c) a server computer, coupled to the communication network and the image storage device, wherein the server computer performs the steps of:
 - (i) pre-processing the digital image through a lossless wavelet transformation;
 - (ii) receiving the coordinates from the client computer; and
 - (iii) progressively transmitting to the client computer the region of interest within the digital image defined by the coordinates.

2. The system of claim 1, wherein the server computer progressively transmits the region of interest to a selected quality threshold.

3. The system of claim 1, wherein the server computer progressively transmits the region of interest to lossless quality.

4. The system of claim 1, wherein the client computer reverse transforms the region of interest received from the server computer, to form a lossless reproduction of the digital image.

5. The system of claim 4, wherein client computer displays the lossless reproduction of the digital image on a web browser resident on the client computer.

6. The system of claim 1, wherein the server computer performs the pre-processing step through a lossless wavelet transformation comprising two non-identical one-dimensional transforms.

7. A system for transmitting a digital image over a communication network, comprising:

- (a) an image storage device for storing a digital image;
- (b) a client computer coupled to the communication network, wherein the client computer generates and transmits across the communication network coordinates defining a region of interest within the digital image;
- (c) a server computer, coupled to the communication network and the image storage device, wherein the server computer performs the steps of:
 - (i) pre-processing the digital image through a lossless wavelet transformation;
 - (ii) generating wavelet coefficients corresponding to the digital image;
 - (iii) generating half-bit flags, each half-bit flag corresponding to a wavelet coefficient;
 - (iv) receiving the coordinates from the client computer;
 - (v) progressively transmitting to the client computer the region of interest within the digital image defined by the coordinates, based on the wavelet coefficients and the corresponding half-bit flags.

8. The system of claim 7, wherein the server computer progressively transmits the region of interest to a selected quality threshold.

9. The system of claim 7, wherein the server computer progressively transmits the region of interest to lossless quality.

10. The system of claim 7, wherein the client computer reverse transforms the region of interest received from the server computer, to form a lossless reproduction of the digital image.

11. The system of claim 10, wherein client computer displays the lossless reproduction of the digital image on a web browser resident on the client computer.

12. The system of claim 7, wherein the server computer performs the pre-processing step through a lossless wavelet transformation comprising two non-identical one-dimensional transforms.

13. A method for transmitting a digital image from a server computer to a client computer, wherein the client computer generates coordinates defining a region of interest within the digital image, and transmits the coordinates to the server computer, the method comprising the steps of:

(a) storing a digital image within an image storage device;

(b) pre-processing the digital image through a lossless wavelet transformation;

(c) receiving the coordinates at the server computer from the client computer; and

(d) progressively transmitting from the server computer to the client computer the region of interest within the digital image defined by the coordinates.

14. The method of claim 13, wherein the server computer progressively transmits the region of interest to a selected quality threshold.

15. The method of claim 13, wherein the server computer progressively transmits the region of interest to lossless quality.

16. The method of claim 13, further comprising the step of reverse transforming at the client computer the region of interest received from the server computer, to form a lossless reproduction of the digital image.

17. The method of claim 16, further comprising the step of displaying at the client computer the lossless reproduction of the digital image on a web browser resident on the client computer.

18. The method of claim 13, wherein the pre-processing step is performed through a lossless wavelet transformation comprising two non-identical one-dimensional transforms.

19. A method for transmitting a digital image from a server computer to a client computer, wherein the client computer generates coordinates defining a region of interest within the digital image, and transmits the coordinates to the server computer, the method comprising the steps of:

- (a) storing a digital image within an image storage device;
- (b) pre-processing the digital image through a lossless wavelet transformation;
- (c) receiving the coordinates at the server computer from the client computer; and
- (d) generating wavelet coefficients corresponding to the digital image;
- (e) generating half-bit flags, each half-bit flag corresponding to a wavelet coefficient;

(f) receiving the coordinates at the server computer from the client computer; and

(g) progressively transmitting from the server computer to the client computer the region of interest within the digital image defined by the coordinates, based on the wavelet coefficients and the corresponding half-bit flags.

20. The method of claim 19, wherein the server computer progressively transmits the region of interest to a selected quality threshold.

21. The method of claim 19, wherein the server computer progressively transmits the region of interest to lossless quality.

22. The method of claim 19, further comprising the step of reverse transforming at the client computer the region of interest received from the server computer, to form a lossless reproduction of the digital image.

23. The method of claim 22, further comprising the step of displaying at the client computer the lossless reproduction of the digital image on a web browser resident on the client computer.

24. The method of claim 19, wherein the pre-processing step is performed through a lossless wavelet transformation comprising two non-identical one-dimensional transforms.

25. A server computer for transmitting a digital image to a client computer, wherein the client computer generates and transmits to the server computer coordinates defining a region of interest within the digital image, the server computer comprising:

(a) an image storage device for storing the digital image;

(b) a processor for performing the steps of:

- (i) pre-processing the digital image through a lossless wavelet transformation;
- (ii) receiving the coordinates from the client computer; and
- (iii) progressively transmitting to the client computer the region of interest within the digital image defined by the coordinates.

26. The system of claim 25, wherein the server computer progressively transmits the region of interest to a selected quality threshold.

27. The system of claim 25, wherein the server computer progressively transmits the region of interest to lossless quality.

28. The system of claim 25, wherein the client computer reverse transforms the region of interest received from the server computer, to form a lossless reproduction of the digital image.

29. The system of claim 28, wherein client computer displays the lossless reproduction of the digital image on a web browser resident on the client computer.

30. The system of claim 25, wherein the server computer performs the pre-processing step through a lossless wavelet transformation comprising two non-identical one-dimensional transforms.

31. A server computer for transmitting a digital image to a client computer, wherein the client computer generates and transmits to the server computer coordinates defining a region of interest within the digital image, the server computer comprising:

- (a) an image storage device for storing the digital image;

(b) a processor for performing the steps of:

- (i) pre-processing the digital image through a lossless wavelet transformation;
- (ii) generating wavelet coefficients corresponding to the digital image;
- (iii) generating half-bit flags, each half-bit flag corresponding to a wavelet coefficient;
- (iv) receiving the coordinates from the client computer;
- (v) progressively transmitting to the client computer the region of interest within the digital image defined by the coordinates, based on the wavelet coefficients and the corresponding half-bit flags.

32. The system of claim 31, wherein the server computer progressively transmits the region of interest to a selected quality threshold.

33. The system of claim 31, wherein the server computer progressively transmits the region of interest to lossless quality.

34. The system of claim 31, wherein the client computer reverse transforms the region of interest received from the server computer, to form a lossless reproduction of the digital image.

35. The system of claim 34, wherein client computer displays the lossless reproduction of the digital image on a web browser resident on the client computer.

36. The system of claim 31, wherein the server computer performs the pre-processing step through a lossless wavelet transformation comprising two non-identical one-dimensional transforms.

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SYSTEM ARCHITECTURE BLOCK DIAGRAM

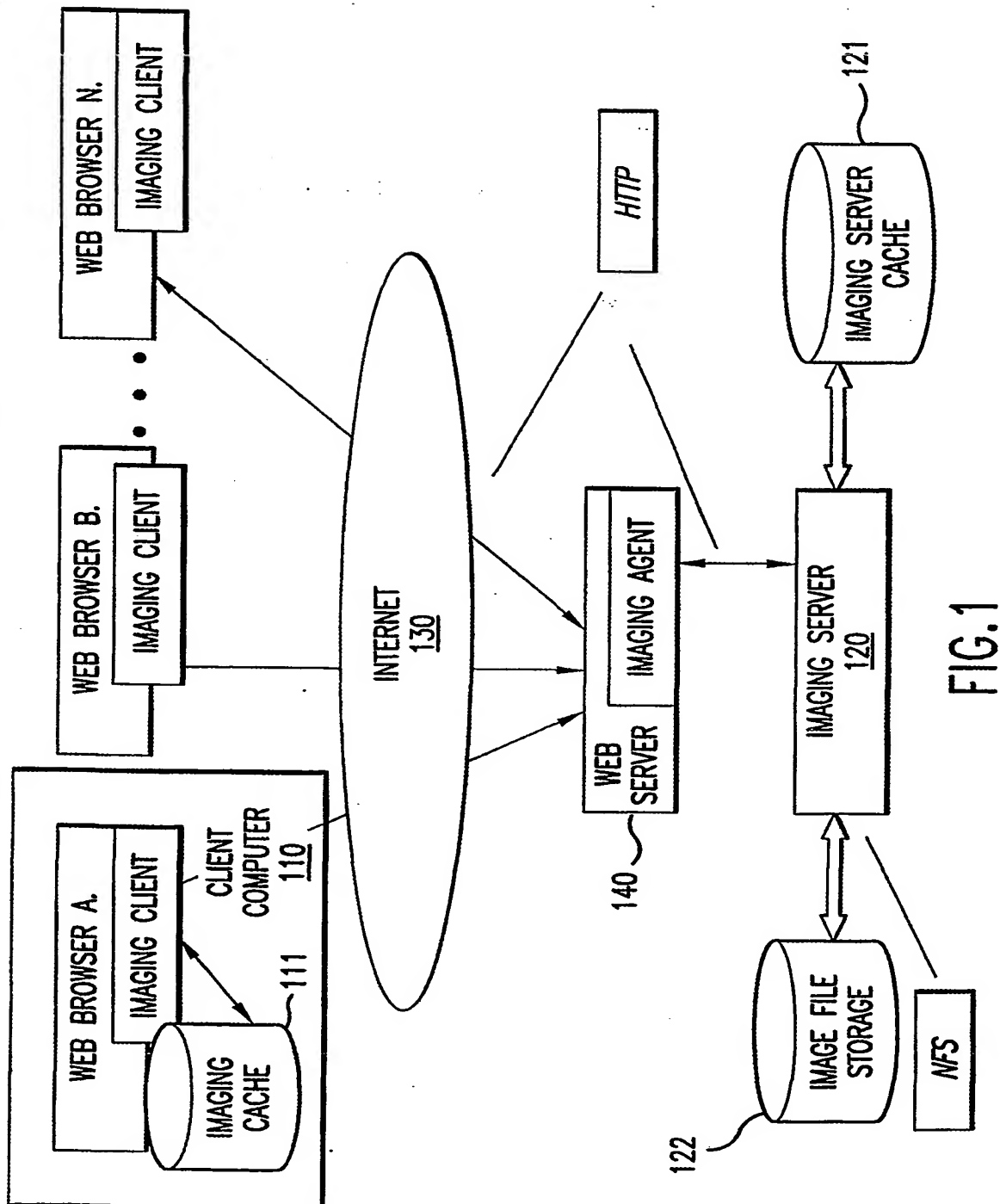


FIG.1

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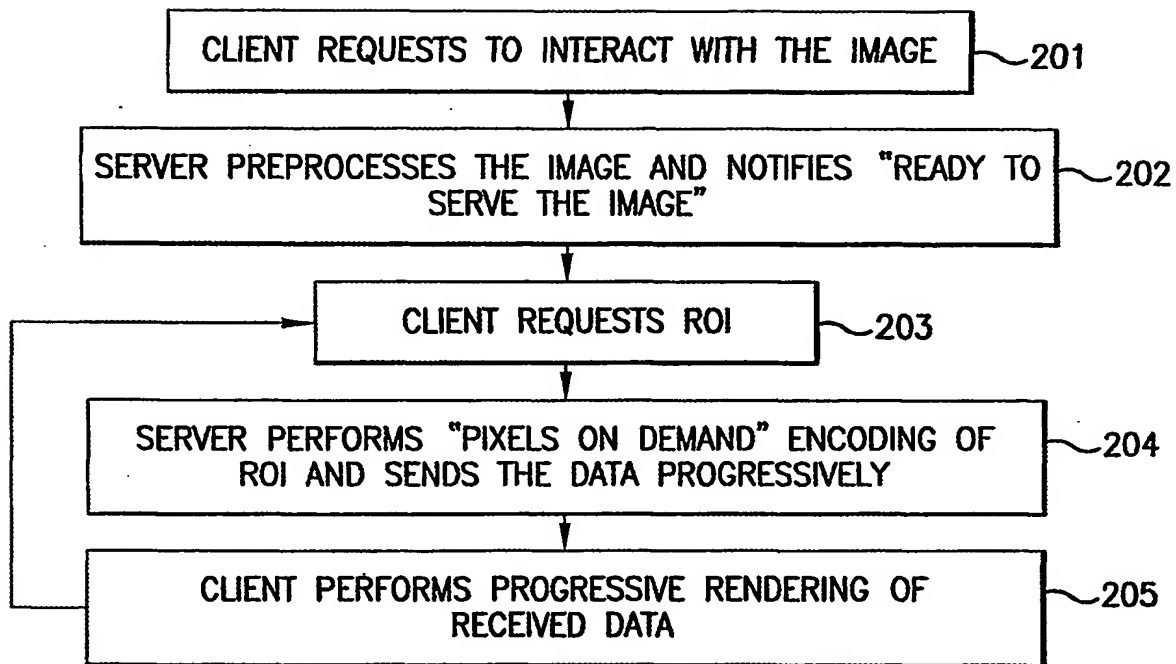


FIG.2

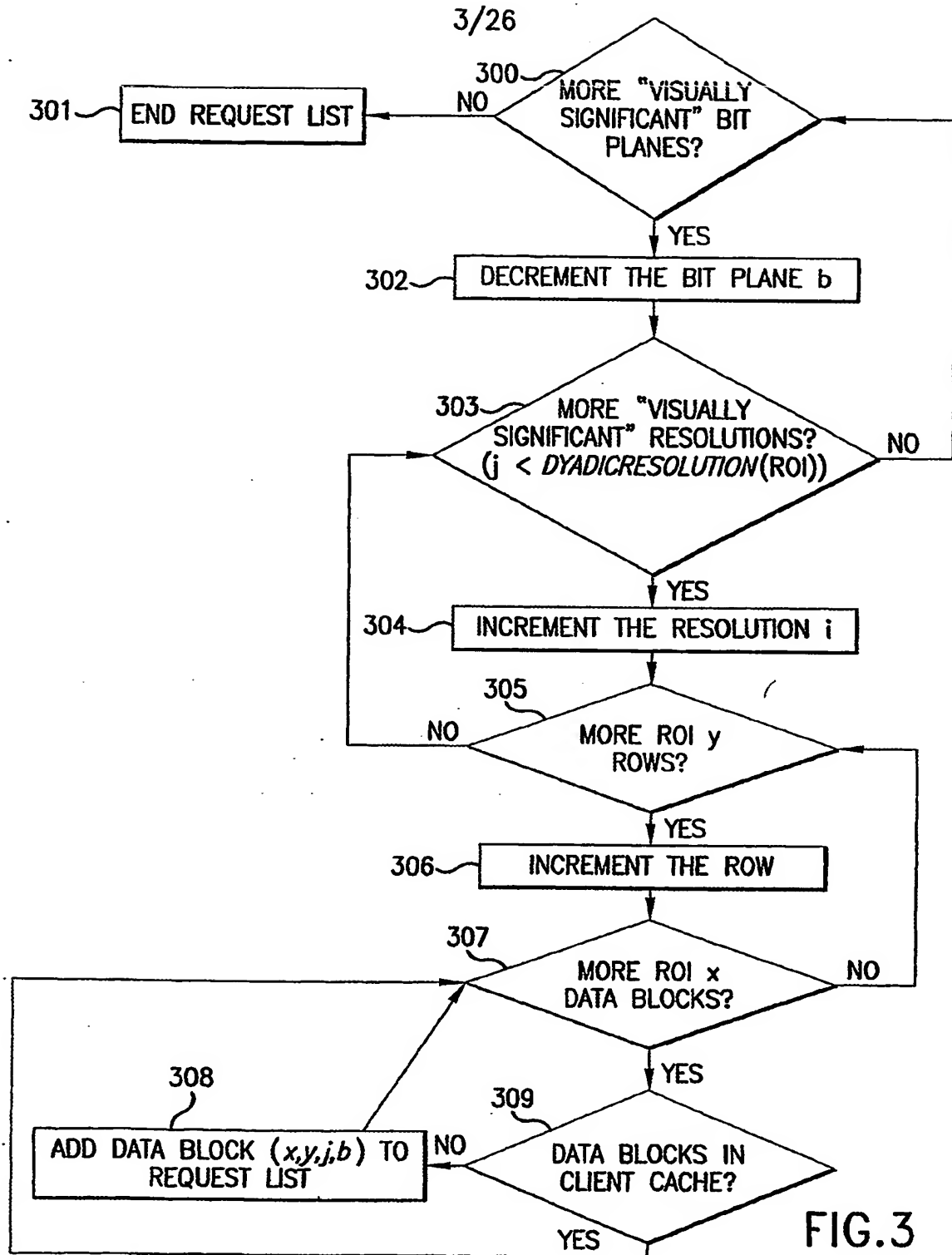


FIG.3

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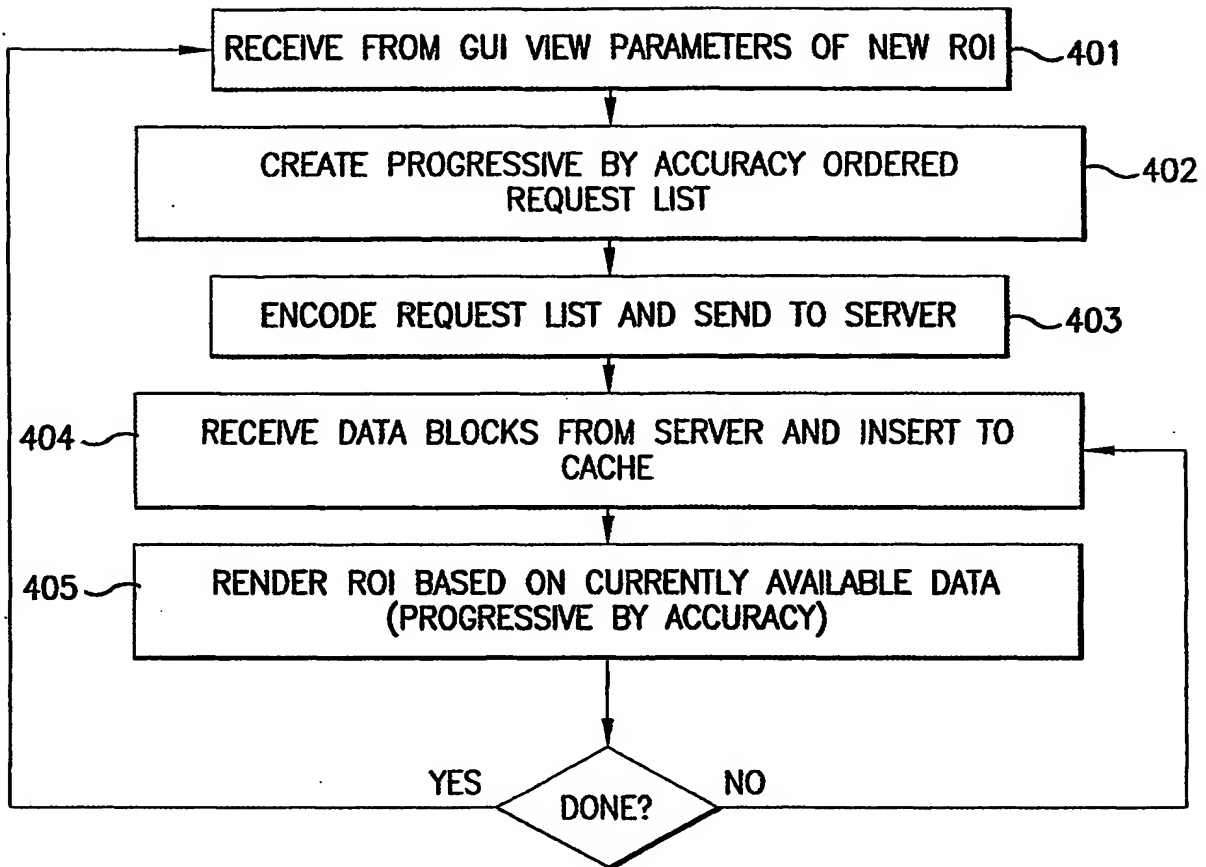


FIG.4

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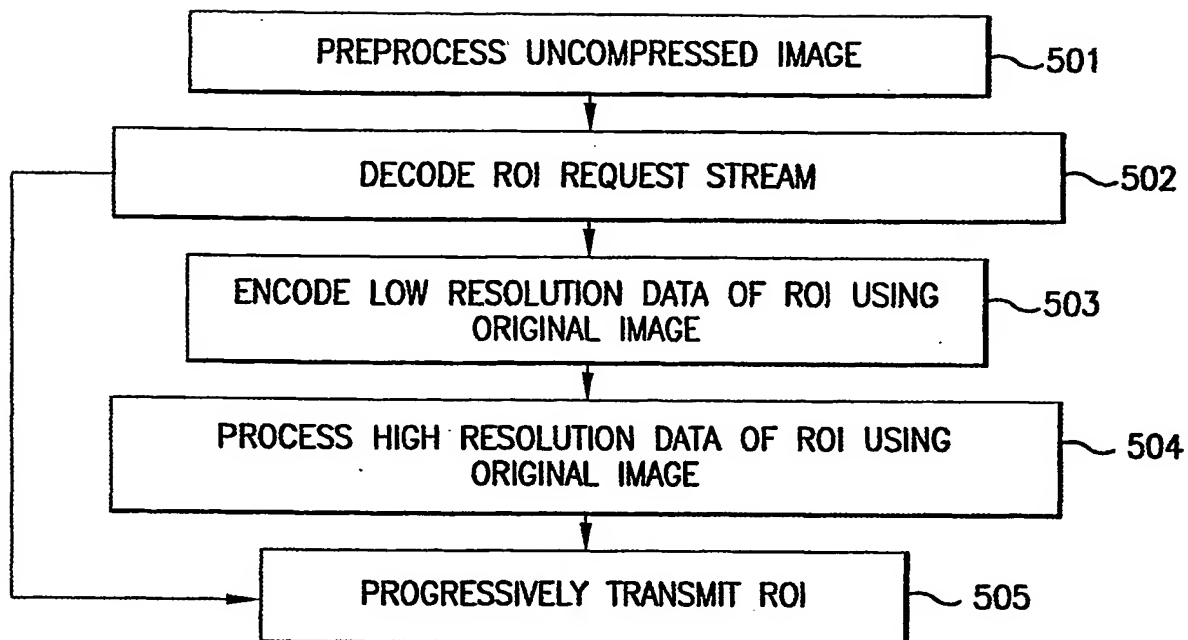


FIG.5

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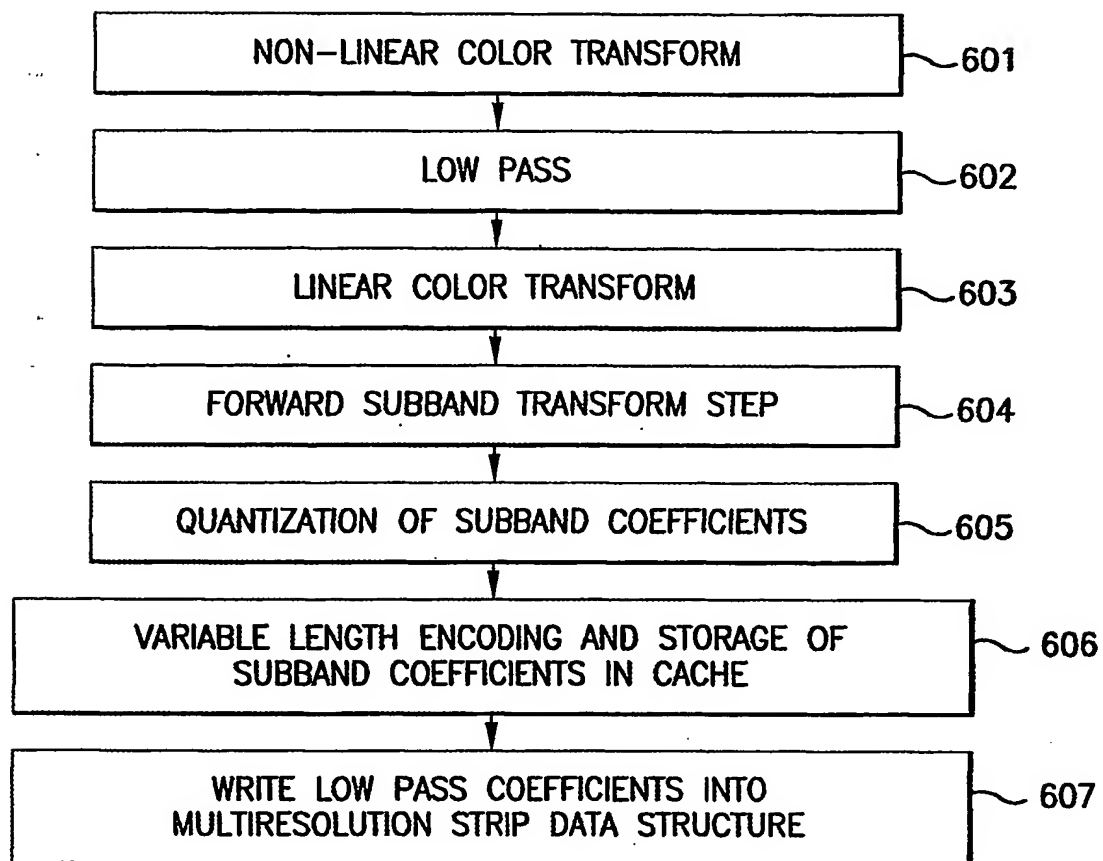


FIG.6

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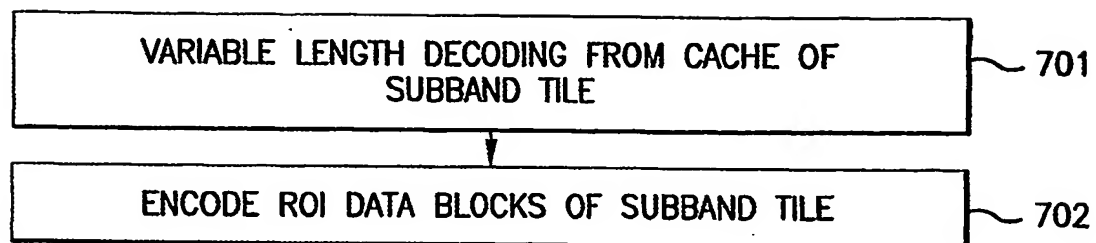


FIG.7

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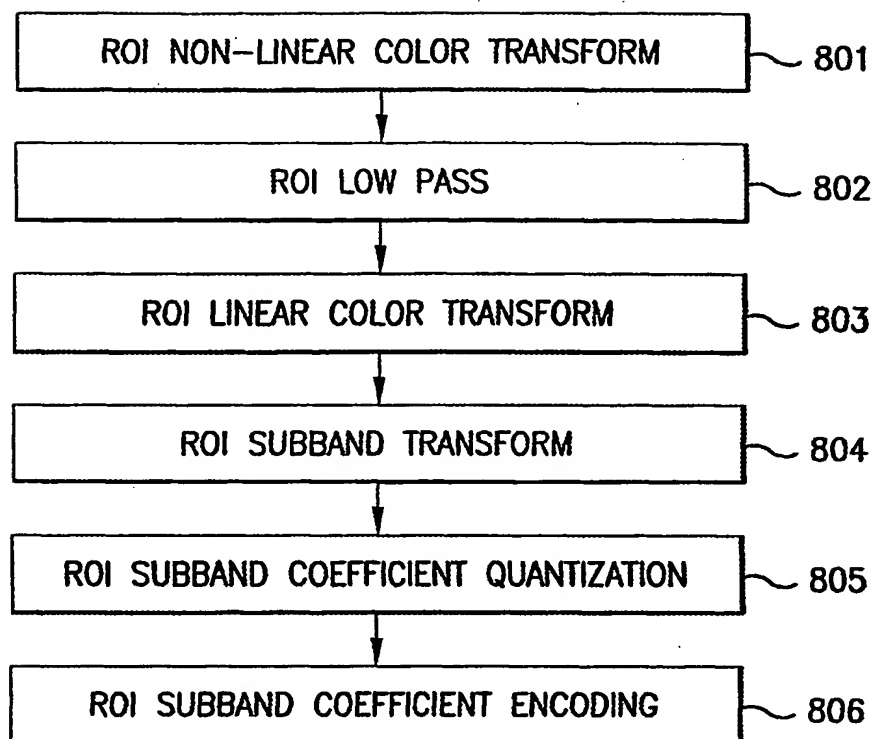


FIG.8

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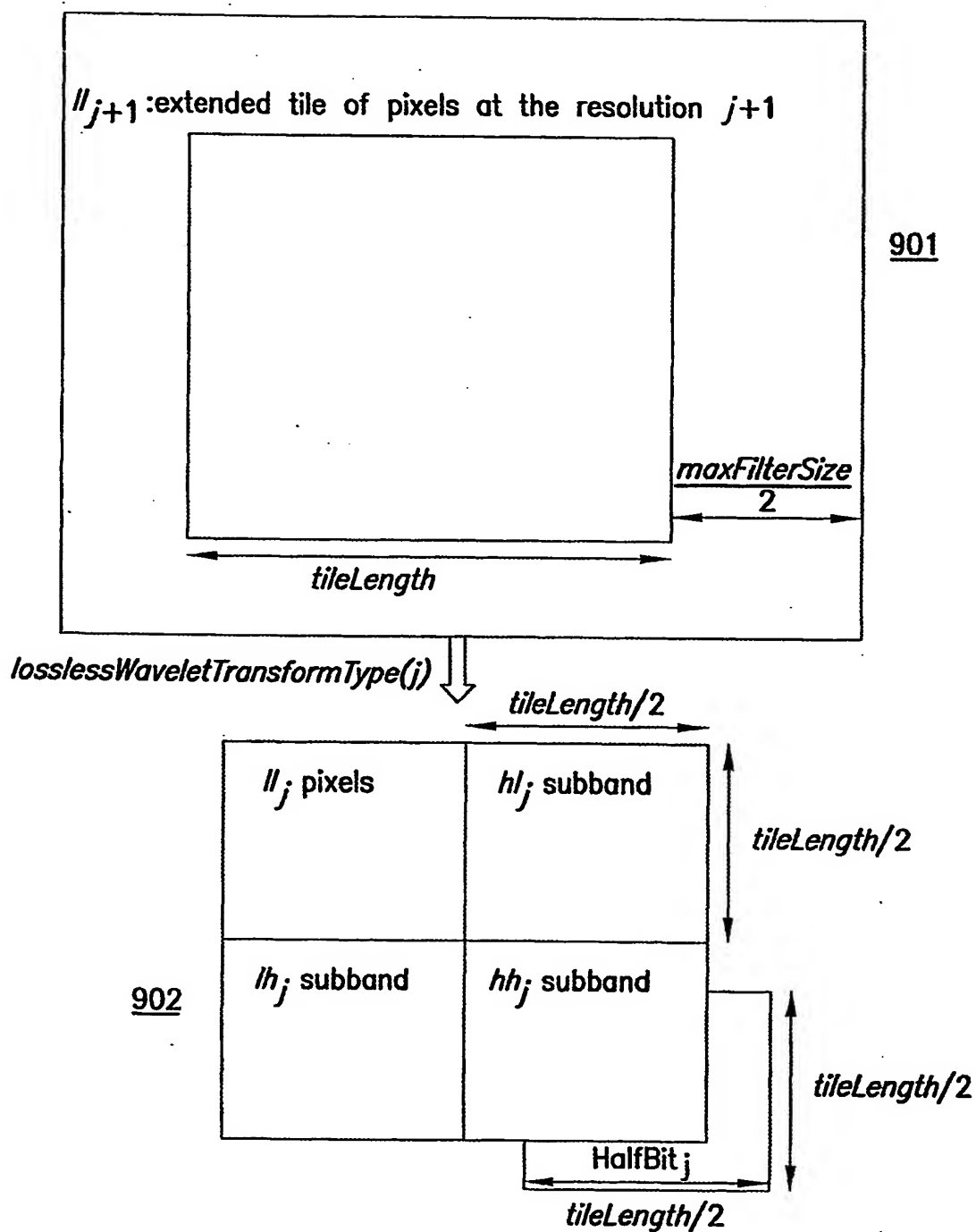


FIG.9

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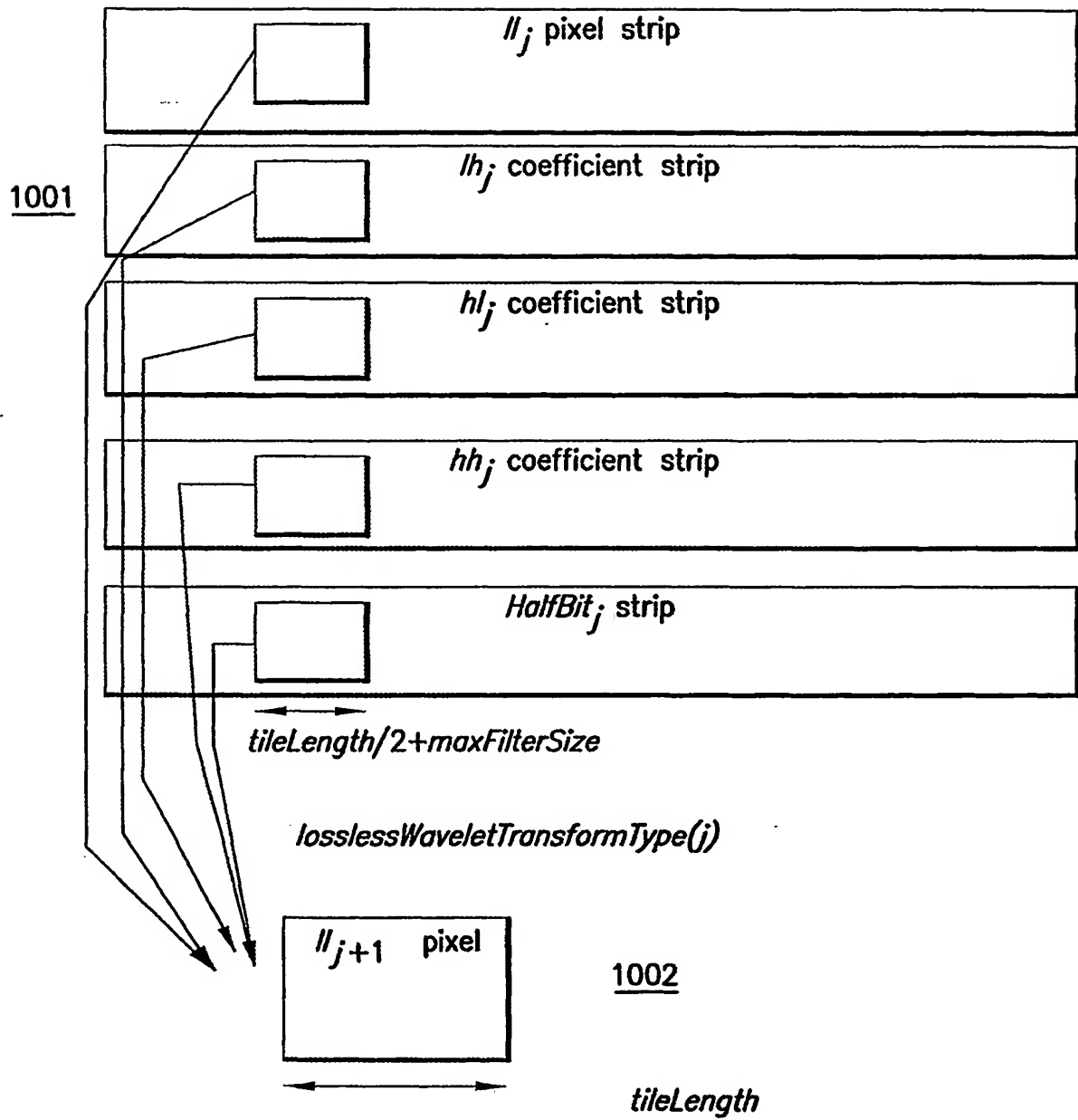


FIG.10

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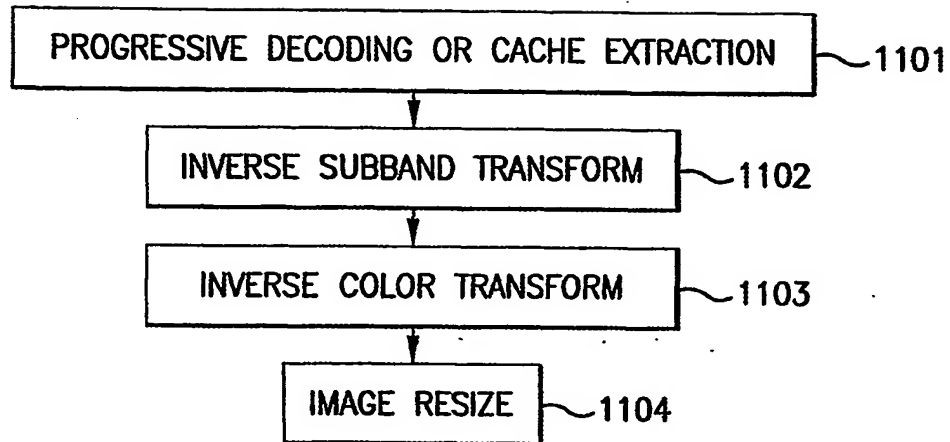


FIG.11

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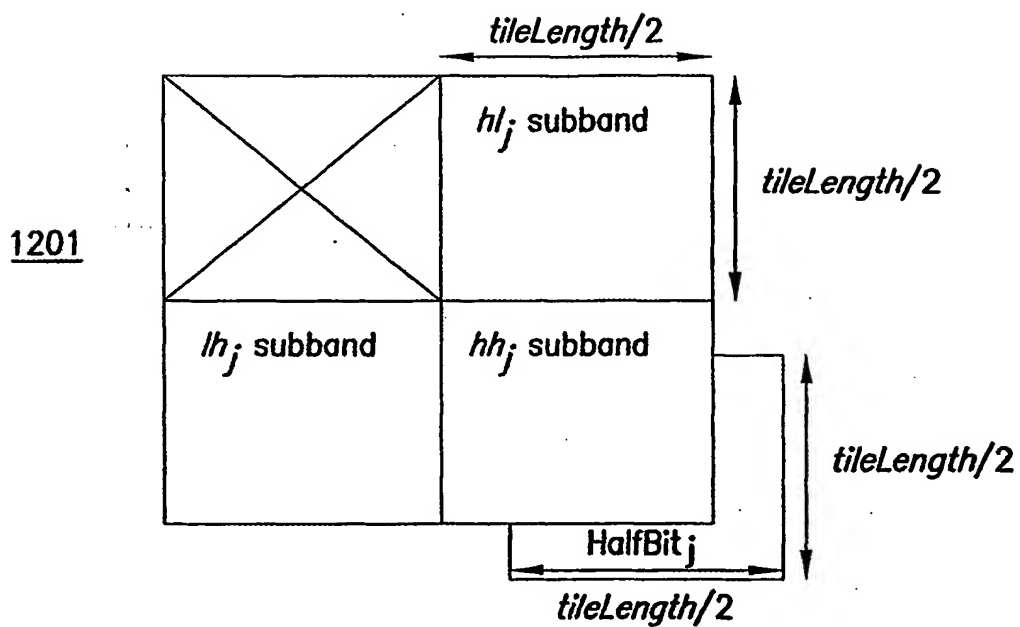


FIG.12

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RGB <-> YUV REVERSIBLE CONVERSION

FORWARD:

$$Y_r = \left\lfloor \frac{R + 2G + B + 2}{4} \right\rfloor$$

$$U_r = R - G$$

$$V_r = B - G$$

INVERSE:

1301

$$G = Y_r - \left\lfloor \frac{U_r + V_r + 2}{4} \right\rfloor$$

$$R = U_r + G$$

$$B = V_r + G$$

FIG.13

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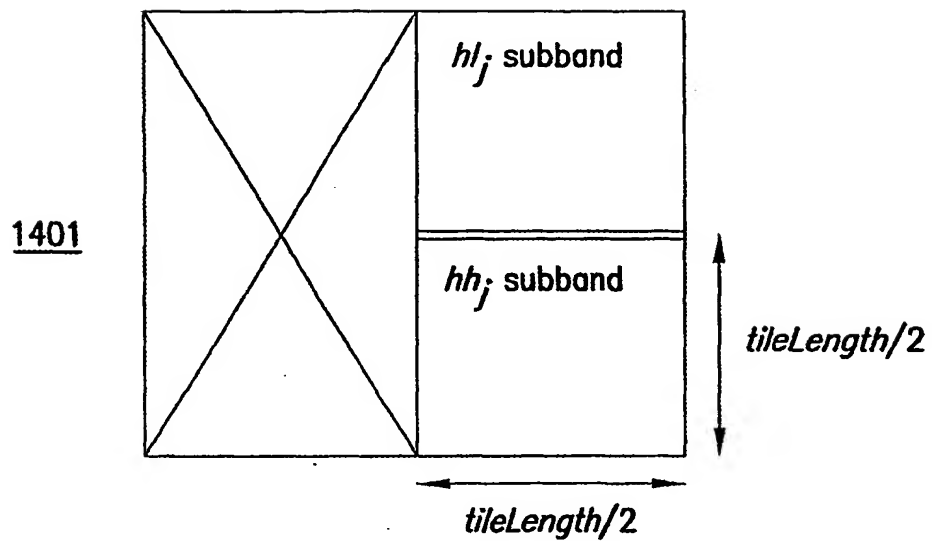


FIG.14

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```

bitModel.startModel () ;
zeroCoefModel.startModel () ;
coefSignModel.startModel () ;

while (encoder.moreCoef ()) {
    if (encoder.isCoefReported ()) {

arithmetic_encode_symbol (bitModel,encoder.reportedCoefPrec
isionBit ()) ;
        }
        else {
            if (encoder.isCoefExactZero ()) ;
                arithmetic_encode_symbol (zeroCoefModel,true) ;
            else {
                arithmetic_encode_symbol (zeroCoefModel,false) ;
                arithmetic_encode_symbol (coefSignModel,encoder.getCoefSign ()) ;
            }
        }
    }
}

```

FIG.15a

```

bitModel.startModel () ;

for (int i = 0 ; i < hBlockSize ; i++) {
    for (int j = 0 ; j < hBlockSize ; j++) {
        arithmetic_encode_symbol (bitModel,
coefHalfBit [i] [j]) ;
    }
}

```

FIG.15b

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```

        bitModel        .startModel() ;
zeroCoefModel.startModel() ;
coefSignModel.startModel() ;

decoder.initializeLSBPlaneCoefScan () ;

while (decoder.moreCoef ()) {
    if (decoder.isCoefReported ()) {
        if (decoder.isLHCoef ()) {
            decoder. updateLSB (0) ;
        }
        else {
            decoder.updateLSB (arithmetic_decoder_symbol (bitModel)) ;
        }
    }
    else {
        if (!decoder.isLHCoef ()) {
            if (!arithmetic_decoder_symbol (zeroCoefModel))
                decoder.setLSB (arithmetic_decoder_symbol (coefSignMode
                    1)) ;
        }
    }
}

```

FIG.16a

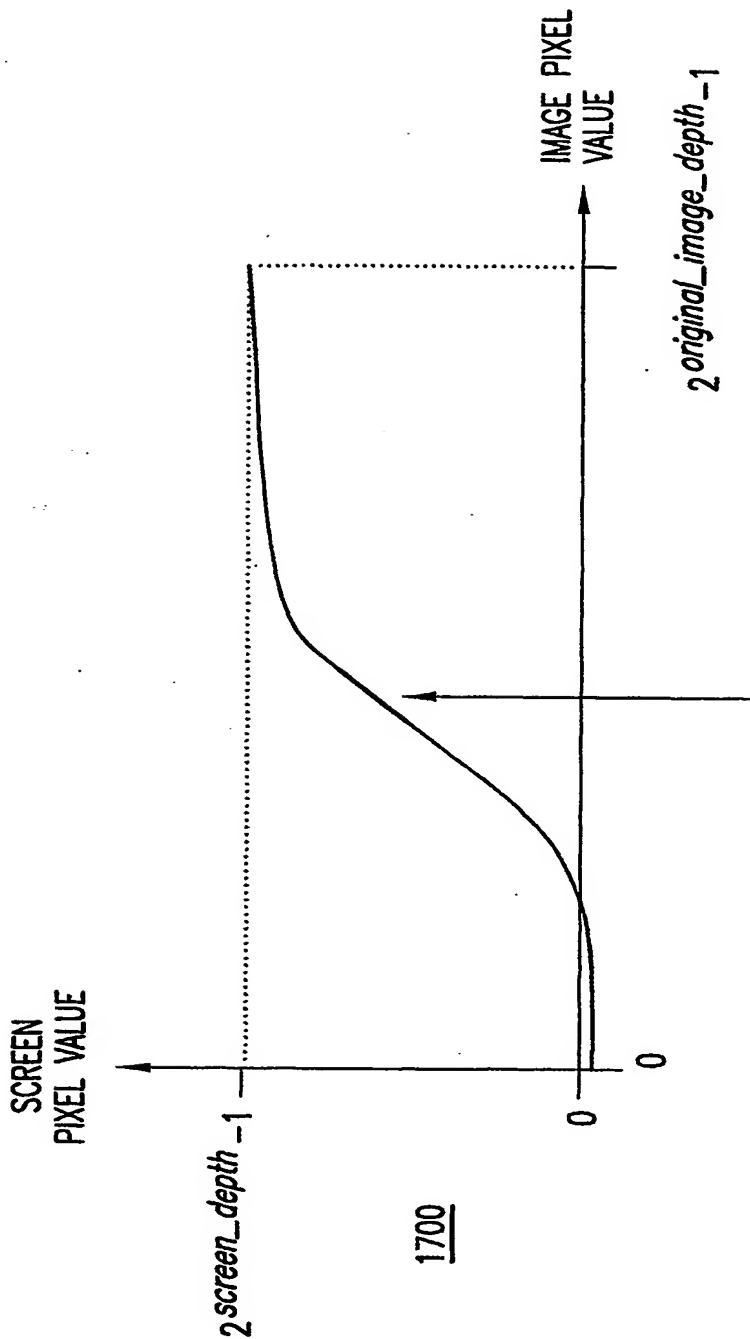
```

bitModel.startModel () ;
for (int i = 0 ; i < hBlockSize ; i++) {
    for (int j = hBlockSize ; j ; j--,p++) {
        coefHlafBit [i] [j] = arithmetic_decoder_symbol (bitModel) ;
    }
}

```

FIG.16b

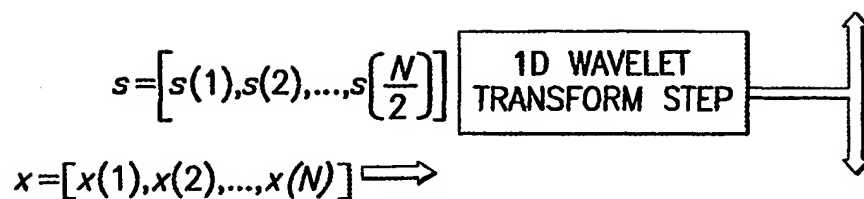
17/26



MAXIMAL GRADIENT
1701

FIG.17

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1800

$$d = [d(1), d(2), \dots, d(\frac{N}{2})]$$

$$X = \begin{bmatrix} x(1,1) & x(1,2) & \dots & x(1,N) \\ x(2,1) & x(2,2) & \dots & x(2,N) \\ \vdots & \vdots & \ddots & \vdots \\ x(M,1) & x(M,2) & \dots & x(M,N) \end{bmatrix}$$

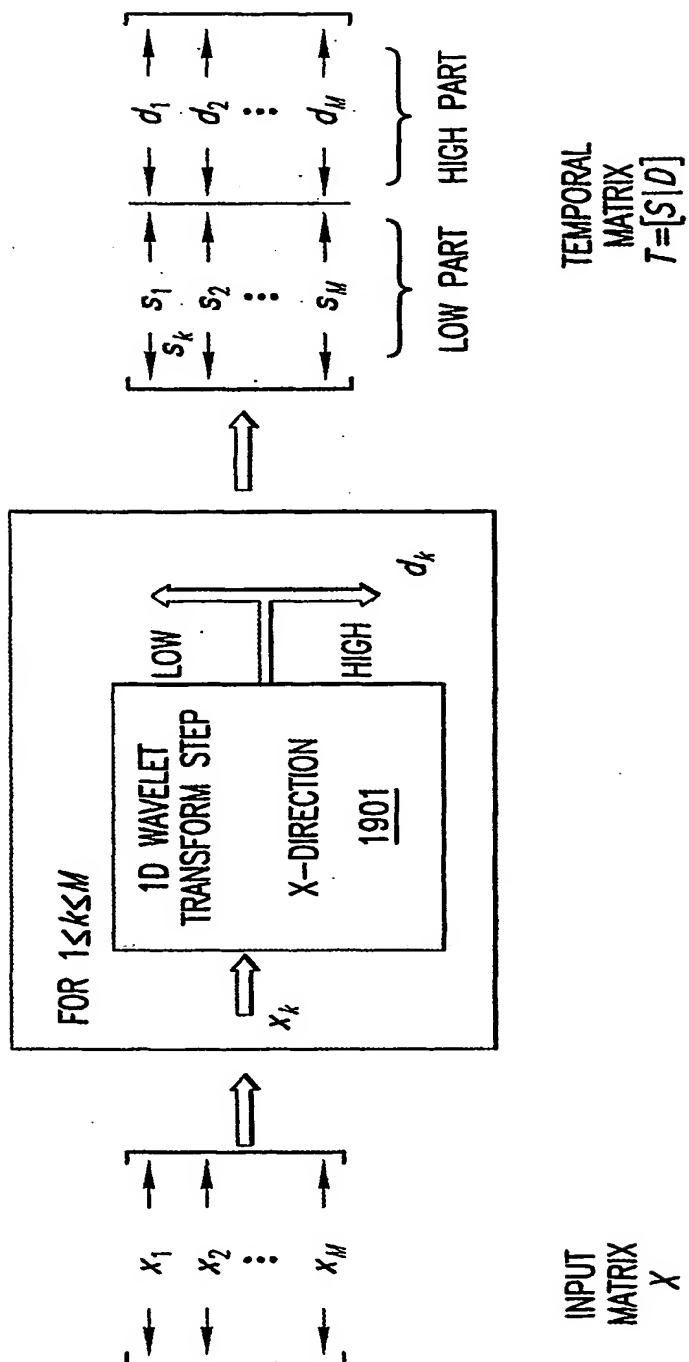
1801

2D WAVELET TRANSFORM STEP

$$\hat{X} = \begin{bmatrix} LL & HL \\ LH & HH \end{bmatrix} = \begin{bmatrix} \begin{matrix} ll(1,1) & \dots & ll(1,N/2) \\ \vdots & \ddots & \vdots \\ ll(M/2,1) & \dots & ll(M/2,N/2) \end{matrix} & \begin{matrix} hl(1,1) & \dots & hl(1,N/2) \\ \vdots & \ddots & \vdots \\ hl(M/2,1) & \dots & hl(M/2,N/2) \end{matrix} \\ \begin{matrix} lh(1,1) & \dots & lh(1,N/2) \\ \vdots & \ddots & \vdots \\ lh(M/2,1) & \dots & lh(M/2,N/2) \end{matrix} & \begin{matrix} hh(1,1) & \dots & hh(1,N/2) \\ \vdots & \ddots & \vdots \\ hh(M/2,1) & \dots & hh(M/2,N/2) \end{matrix} \end{bmatrix}$$

FIG.18

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1901

FIG.19

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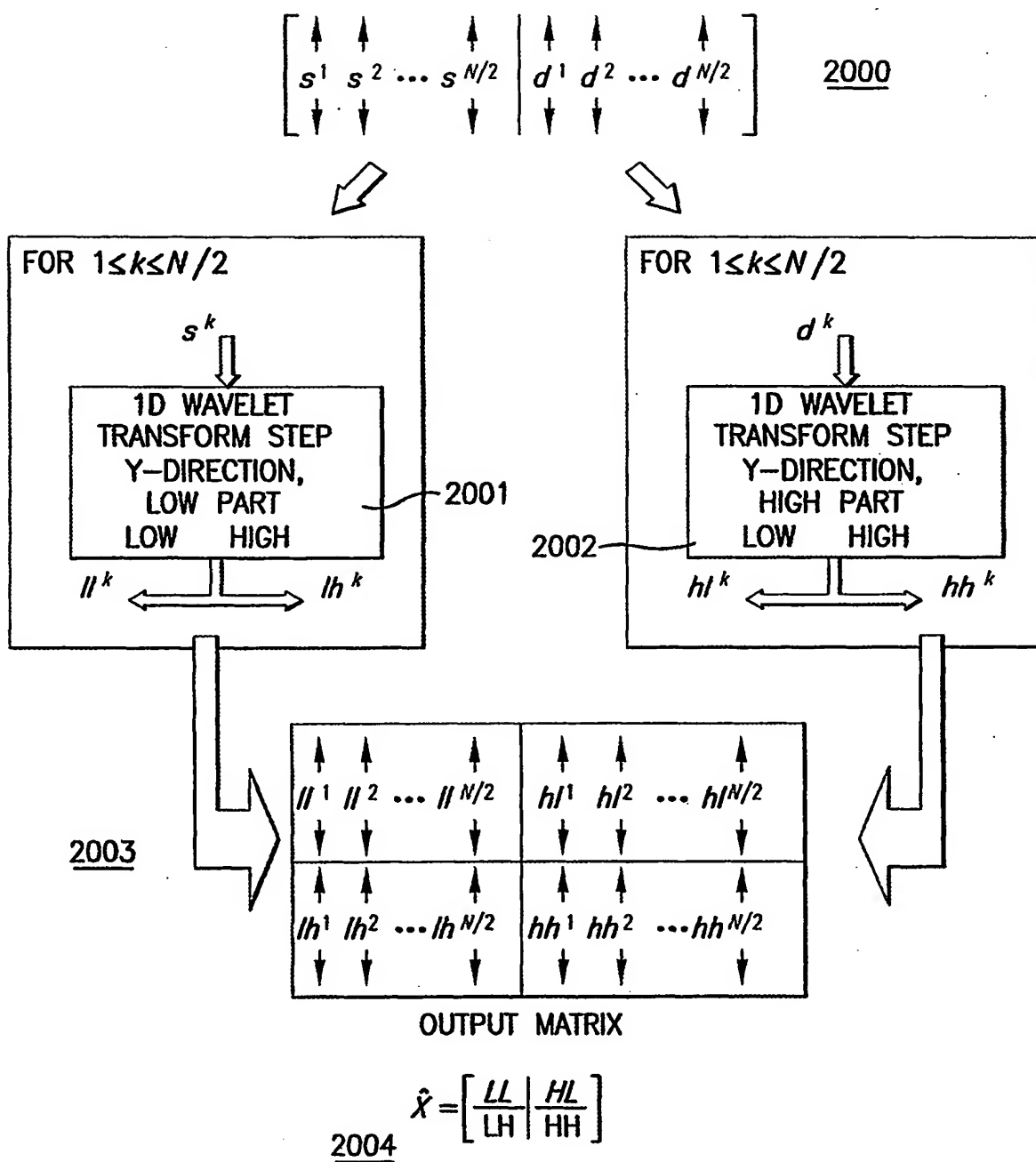


FIG.20

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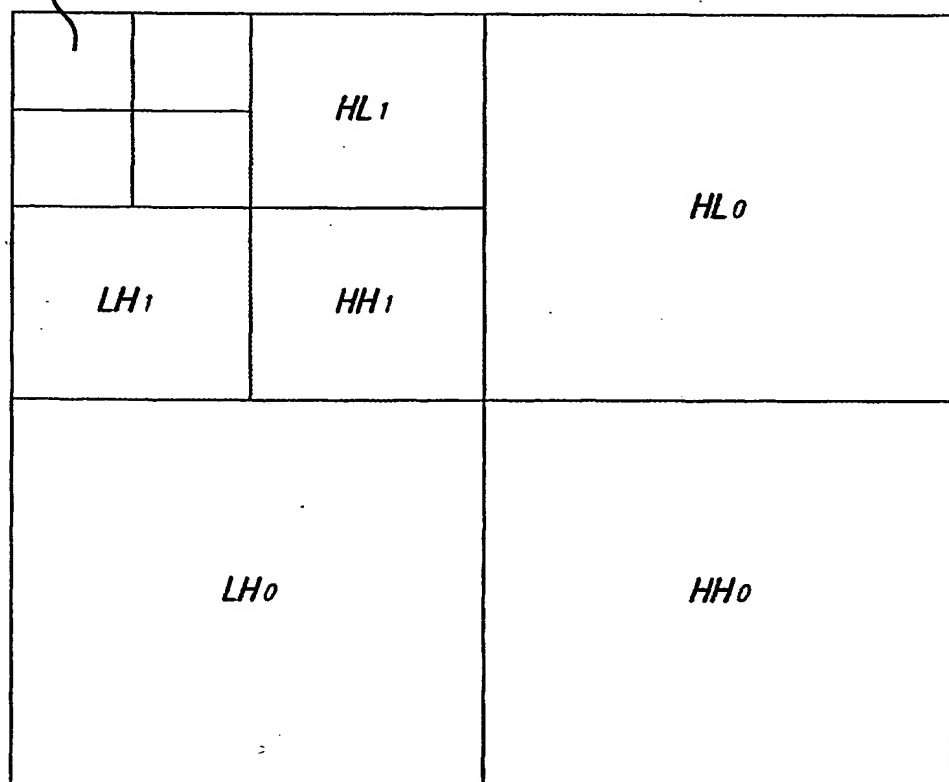
LET I BE THE ORIGINAL IMAGE,FOR $0 < i < \text{LEVELS}$  $LL_{\text{LEVELS}-1}$ 2100

FIG.21

SUBSTITUTE SHEET (RULE 26)

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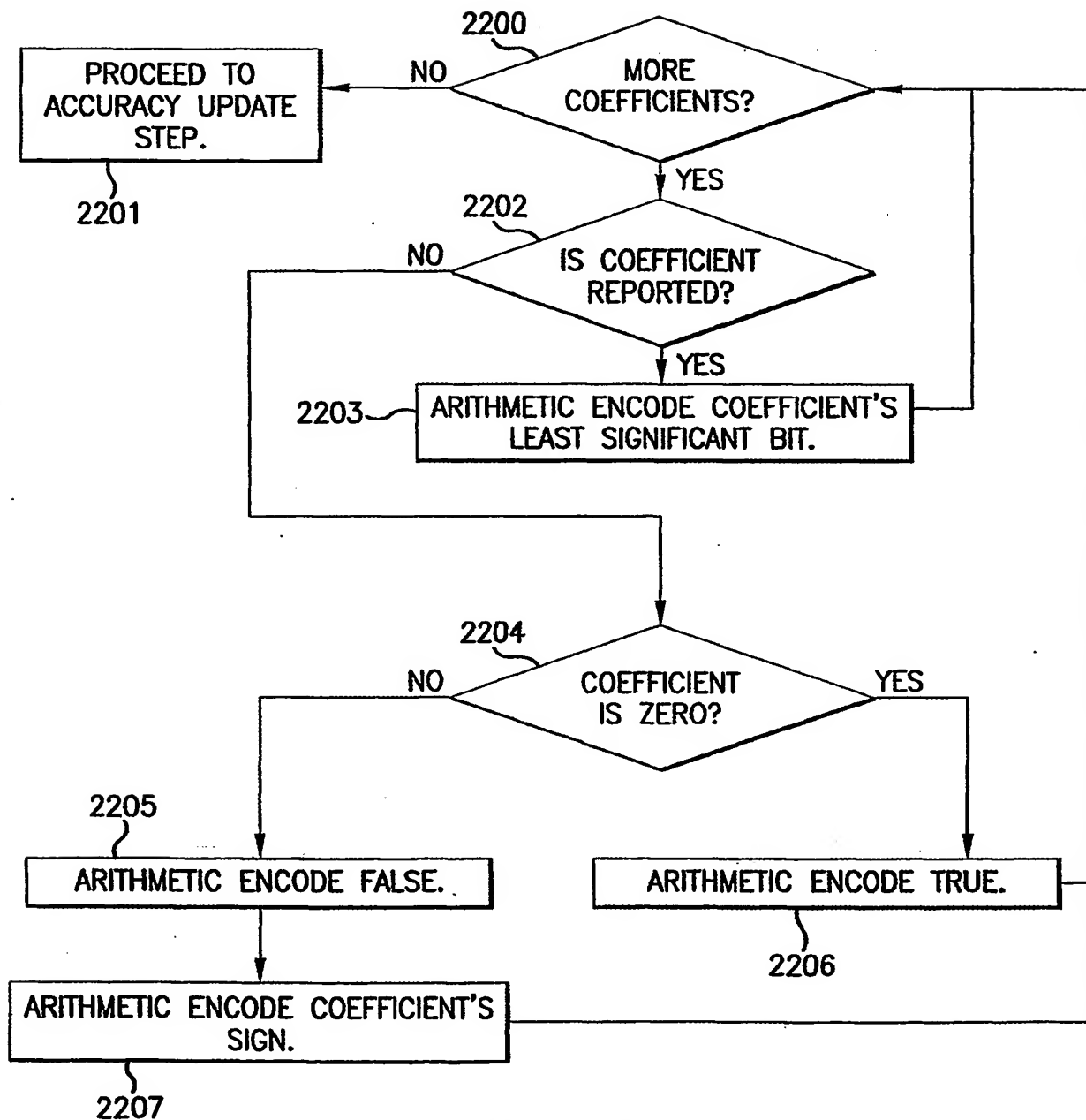


FIG.22

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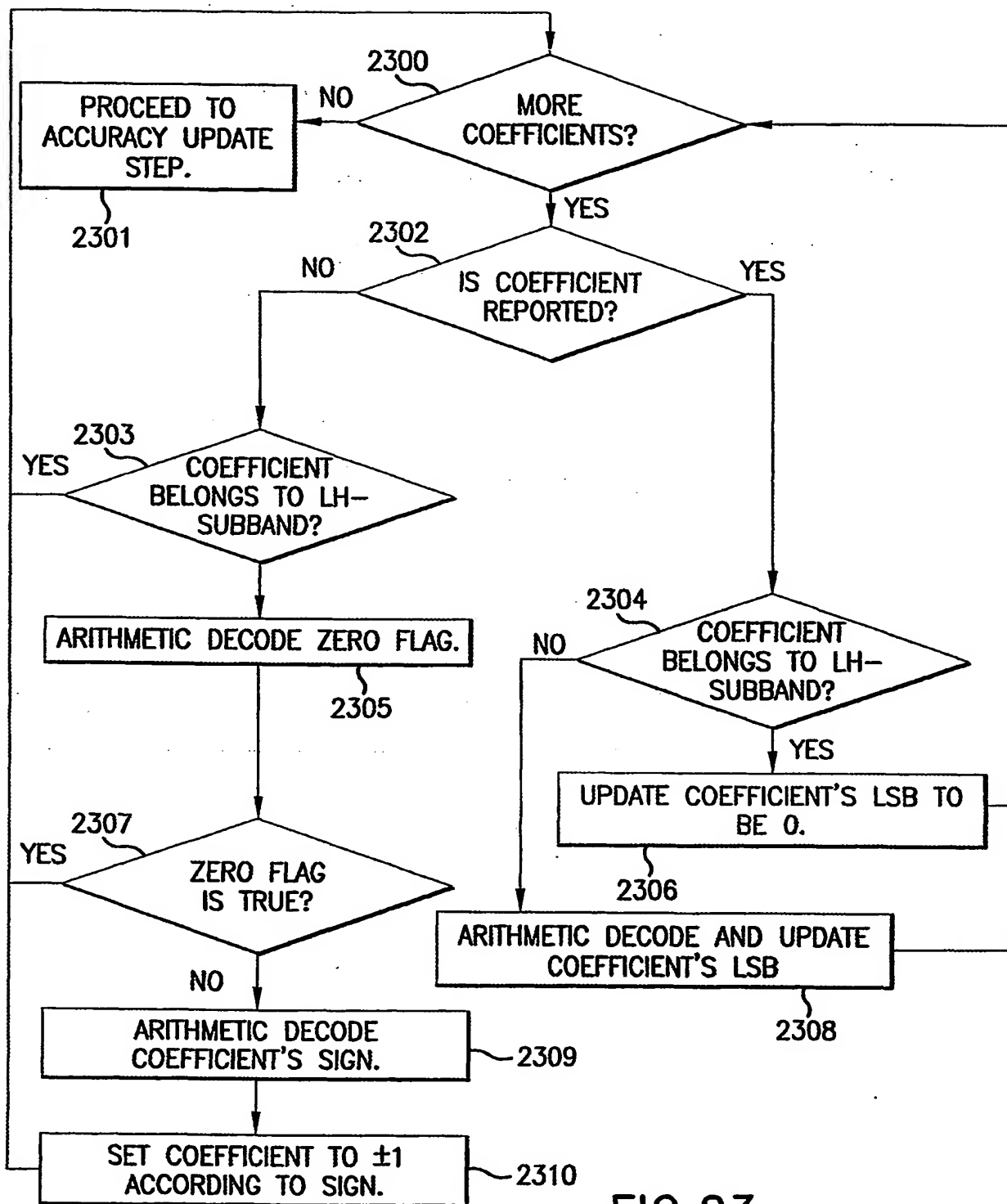
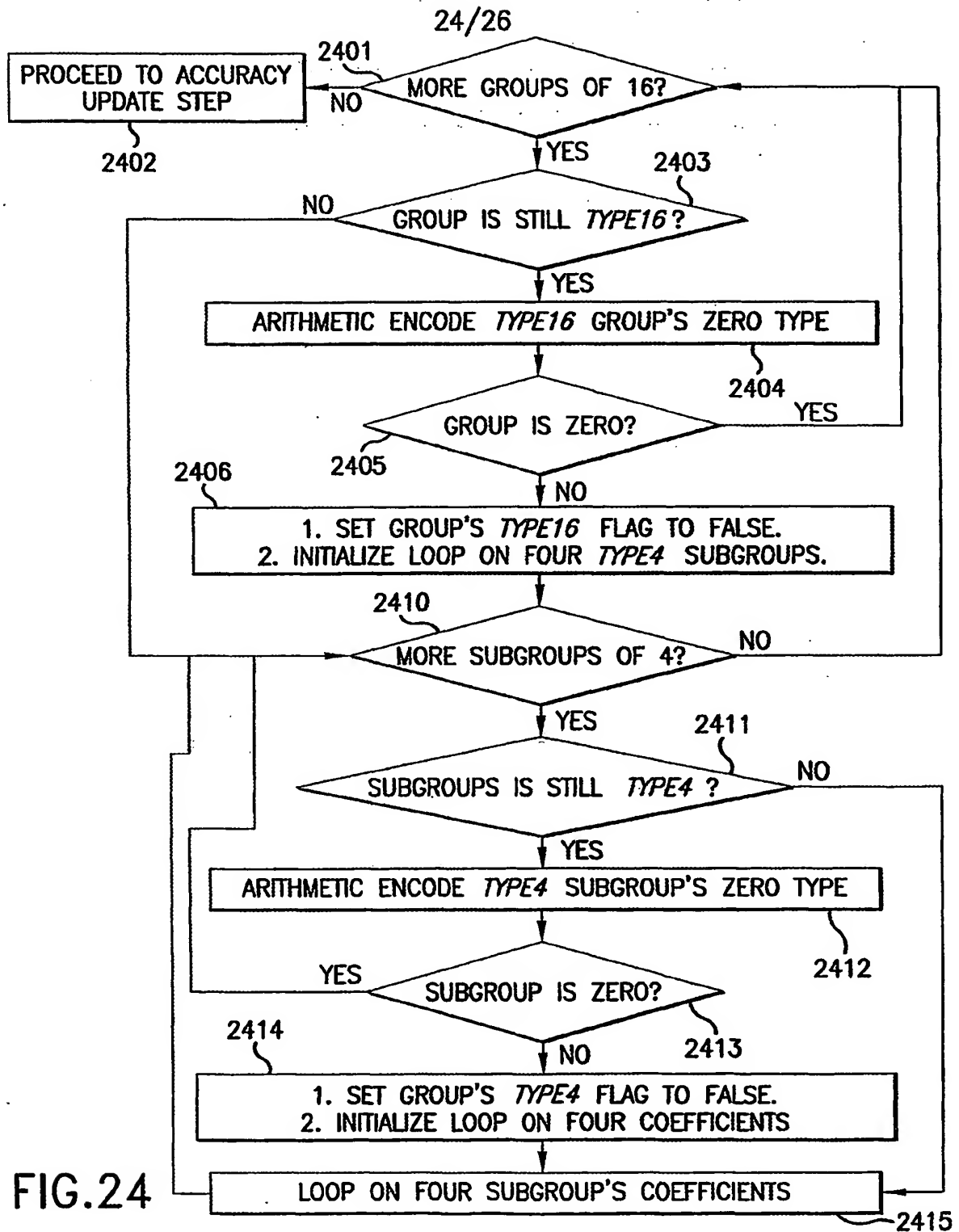


FIG. 23

SUBSTITUTE SHEET (RULE 26)



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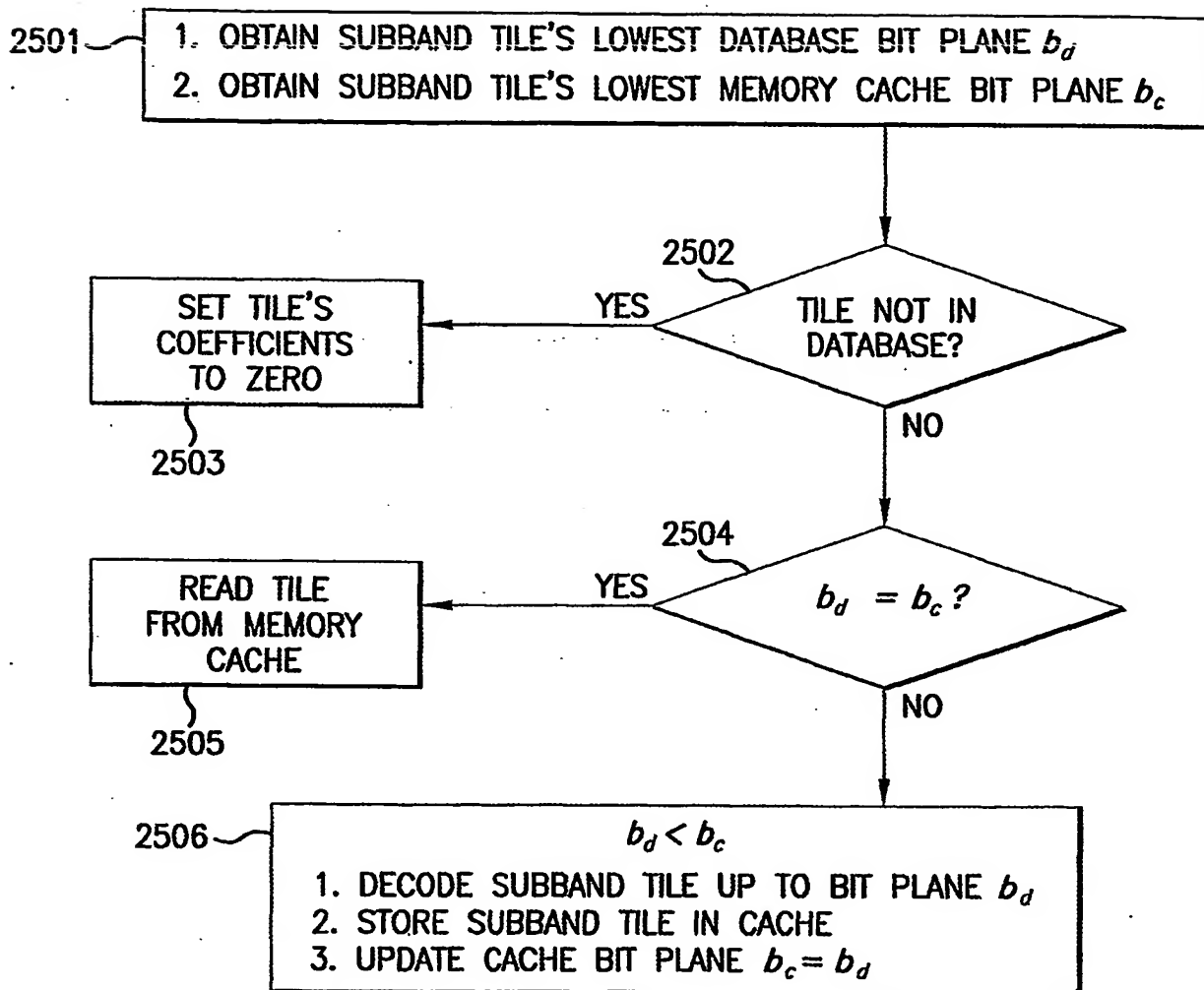
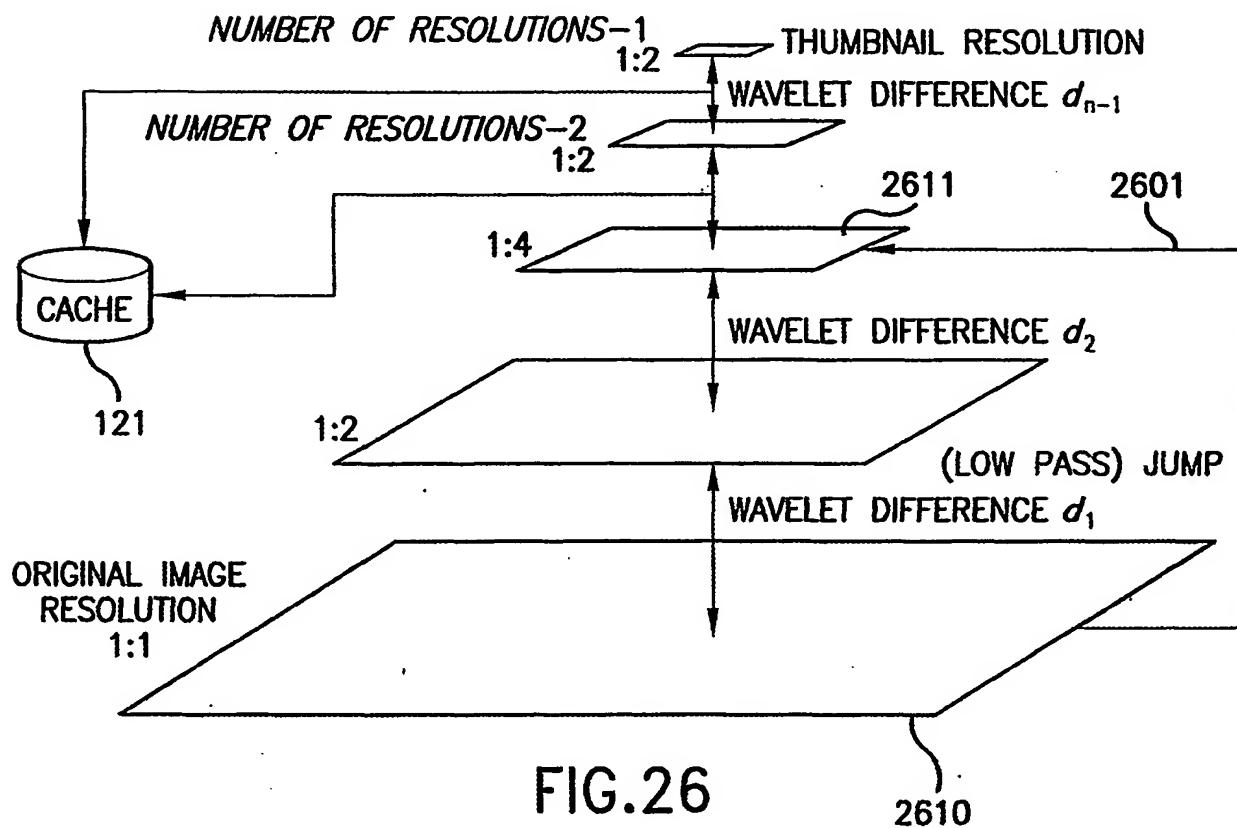


FIG.25

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PREPROCESSING MULTIREOLUTION STRUCTURE



INTERNATIONAL SEARCH REPORT

International application No.
PCT/US01/12390

A. CLASSIFICATION OF SUBJECT MATTER

IPC(7) : H04N 7/12

US CL : 375/240.19

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

U.S. : 375/240.19, 21; 14.08, 14.09, 14.1 348/

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched
NoneElectronic data base consulted during the international search (name of data base and, where practicable, search terms used)
None

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	US 5,872,965 A (PETRICK) 16 February 1999, figs. 2 and 8, col. 5, ln. 26 - col. 6, ln. 51.	1-6, 13-18, 25-30
Y	US 5,838,377 A (GREENE) 17 November 1998, col. 2, ln. 17-27.	1-6, 13-18, 25-30
A	US 5,982,362 A (CRATER et al) 09 November 1999, fig. 2.	1

☐ Further documents are listed in the continuation of Box C.
 ☐ See patent family annex.

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L document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)	*Y* document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art
O document referring to an oral disclosure, use, exhibition or other means	*Z* document member of the same patent family
P document published prior to the international filing date but later than the priority date claimed	

Date of the actual completion of the international search

13 JUNE 2001

Date of mailing of the international search report

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